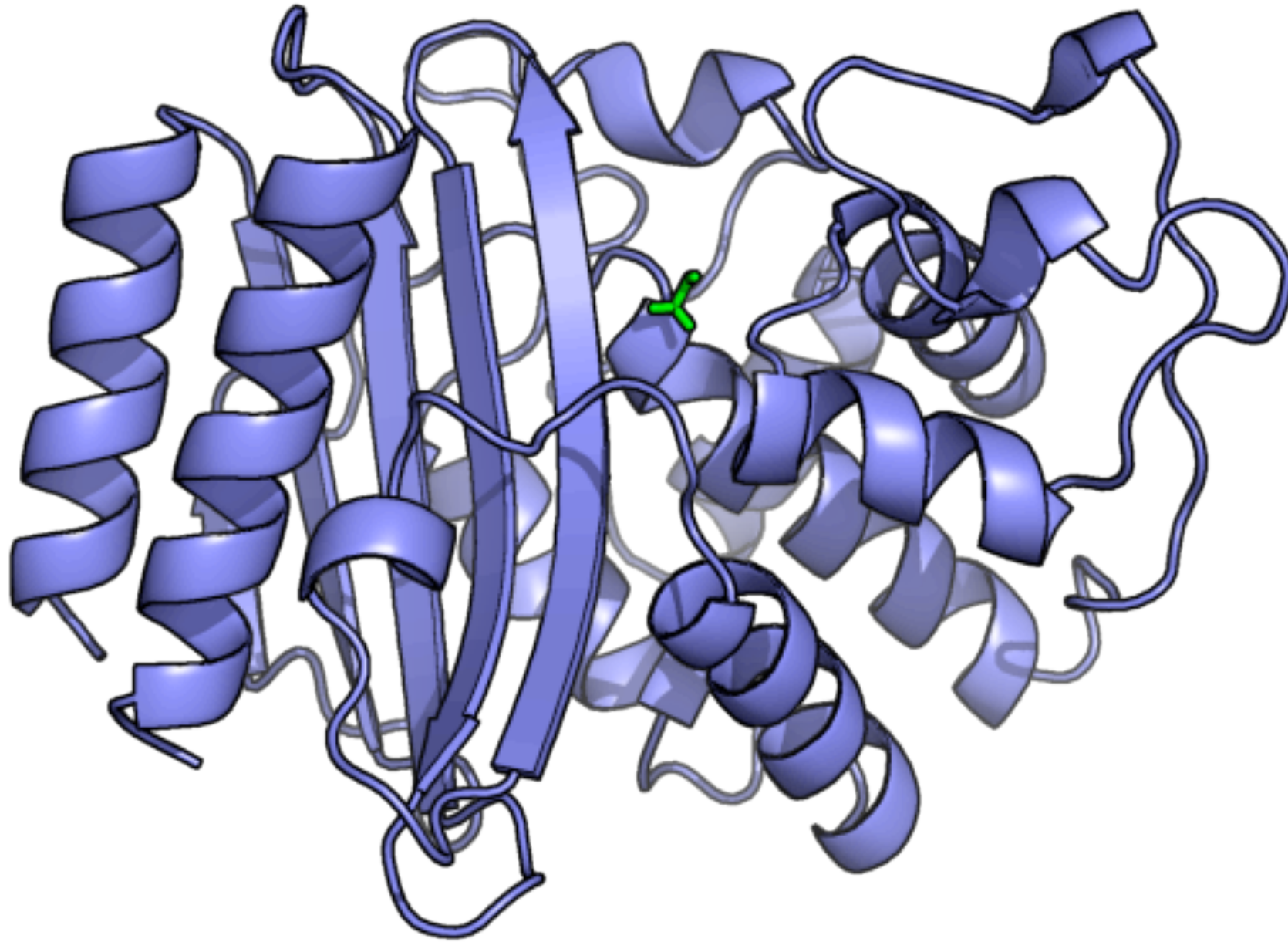


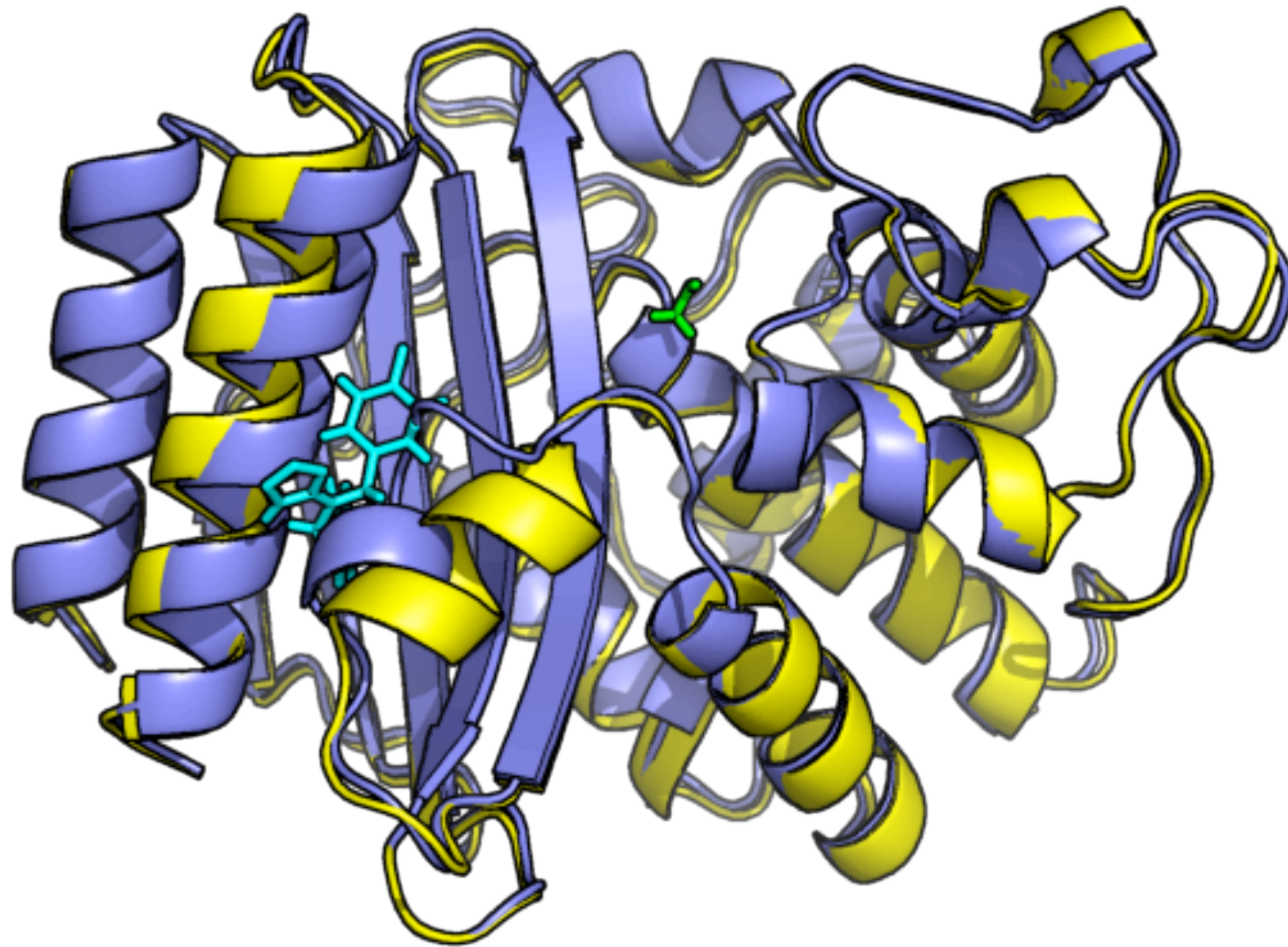
# Augmenting experiments with *in silico* Markov state models

Gregory R. Bowman  
Miller Research Fellow  
University of California, Berkeley

# Meet $\beta$ -lactamase



Considering structural fluctuations opens  
up new possibilities



# Outline

A large, bold black question mark is centered within a white rounded rectangle that has a thin black border. The rectangle is positioned on the left side of the slide.

Computational  
approach

# Outline

?

Computational  
approach

?

Understanding  
and predicting  
allostery

# Outline

?

Computational  
approach

?

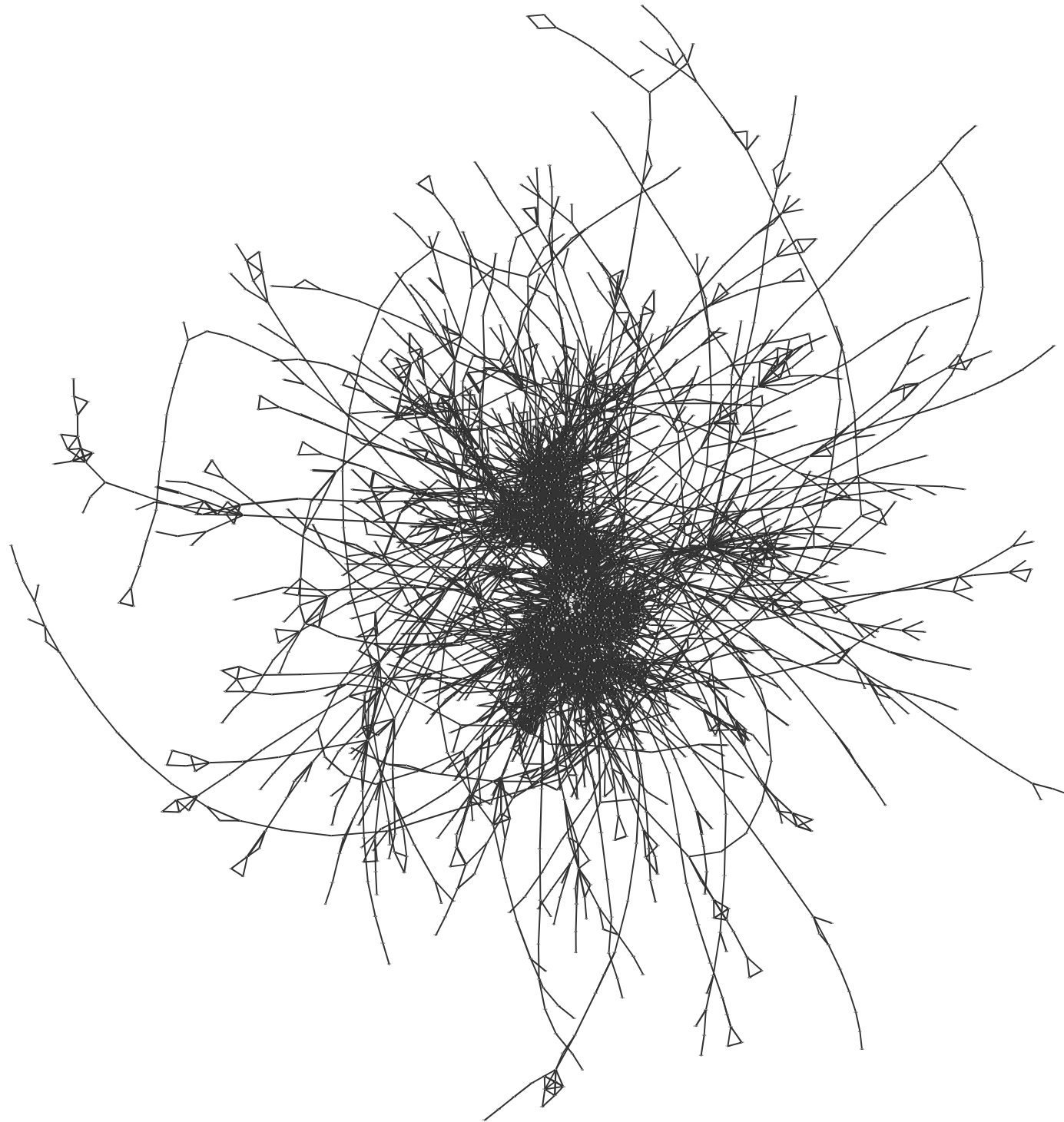
Understanding  
and predicting  
allostery

?

Experimental  
tests

Molecular dynamics simulations capture  
protein fluctuations with atomic  
resolution

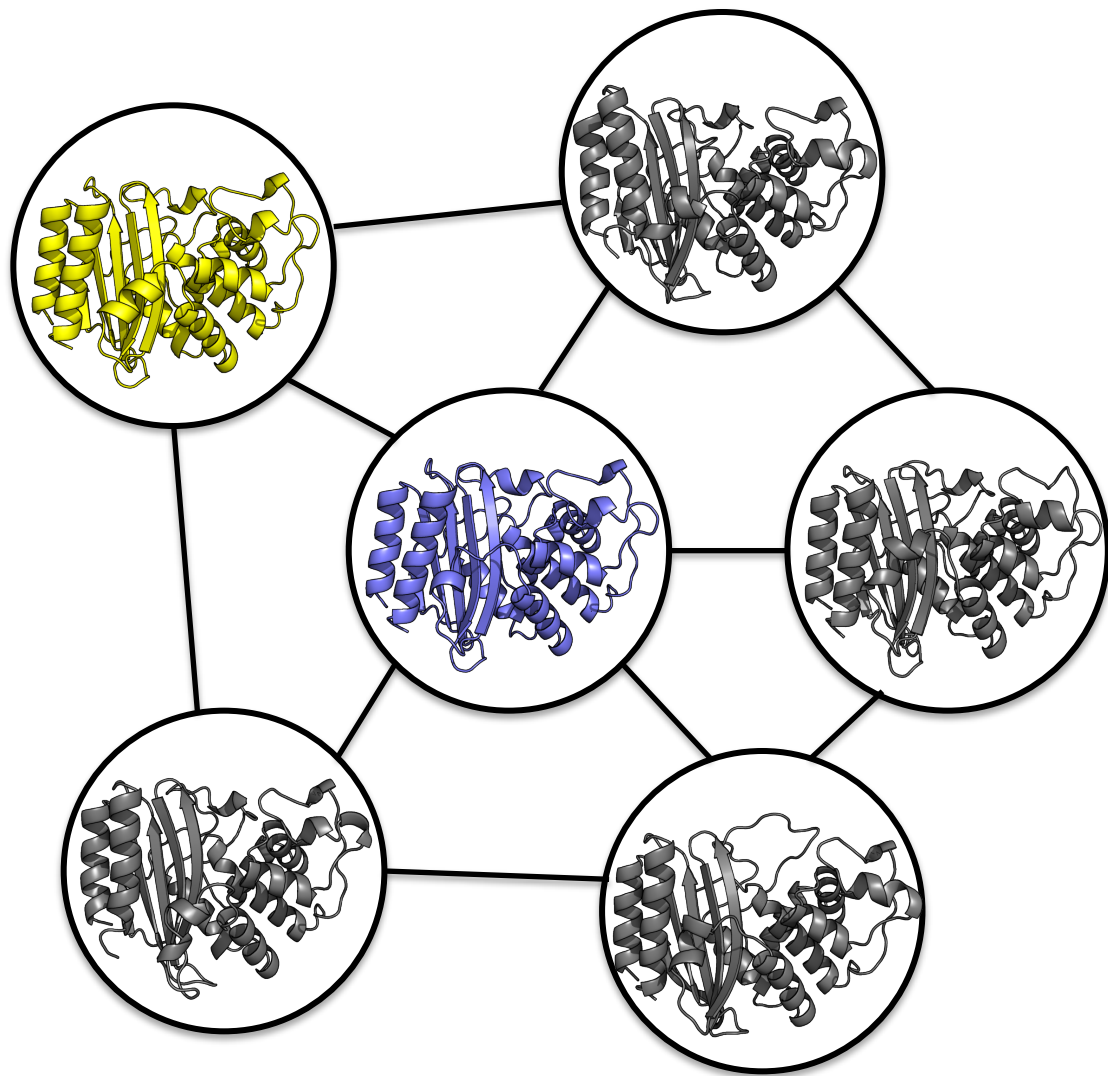
# Markov state models are quantitative maps of a protein's conformational space



Bowman *et al.* Cell Res. 2010.  
Noe *et al.* Curr Opin Struct Biol. 2008.

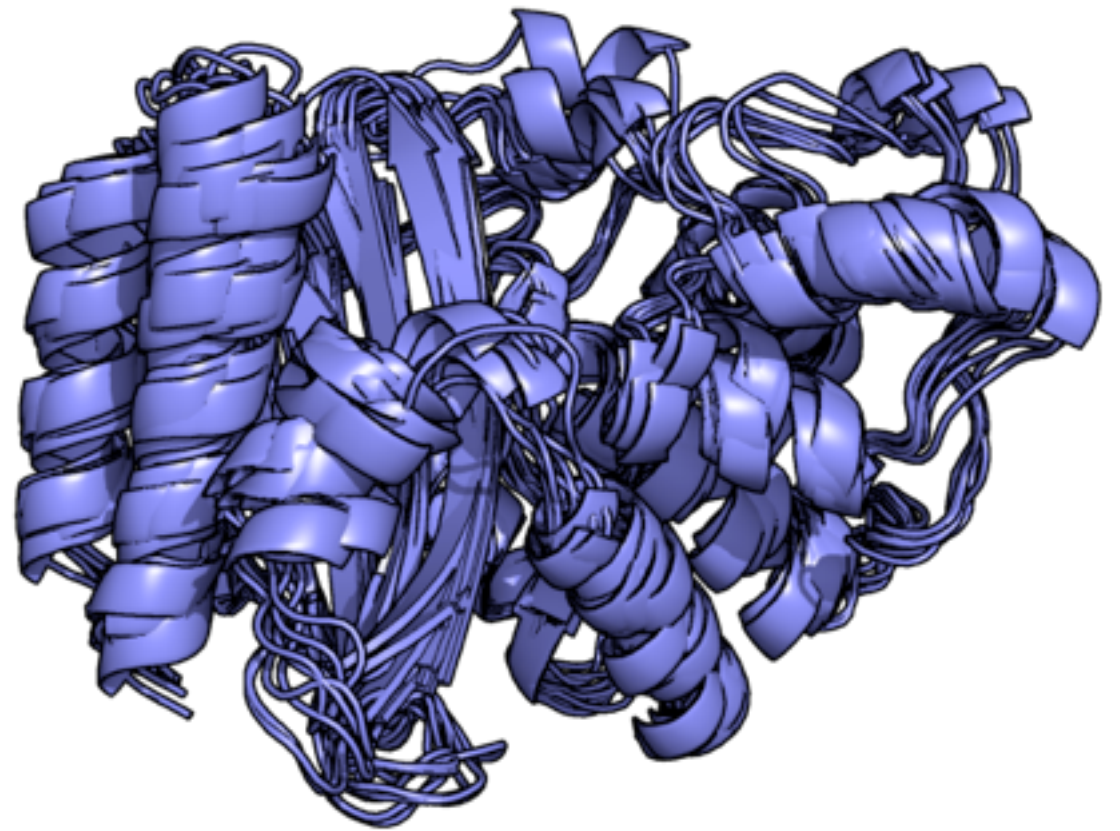
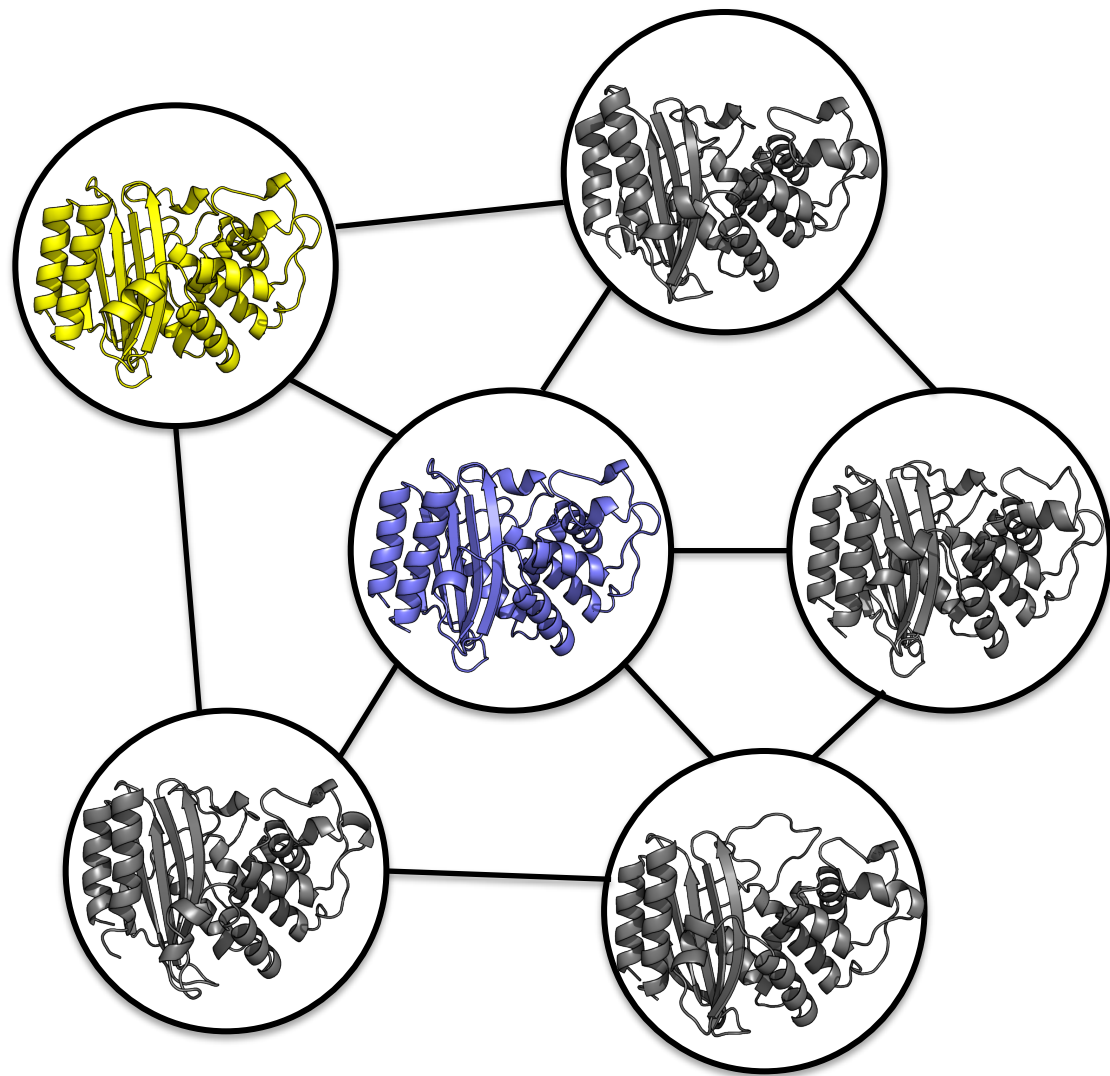


# Coarse-graining Markov models facilitates understanding



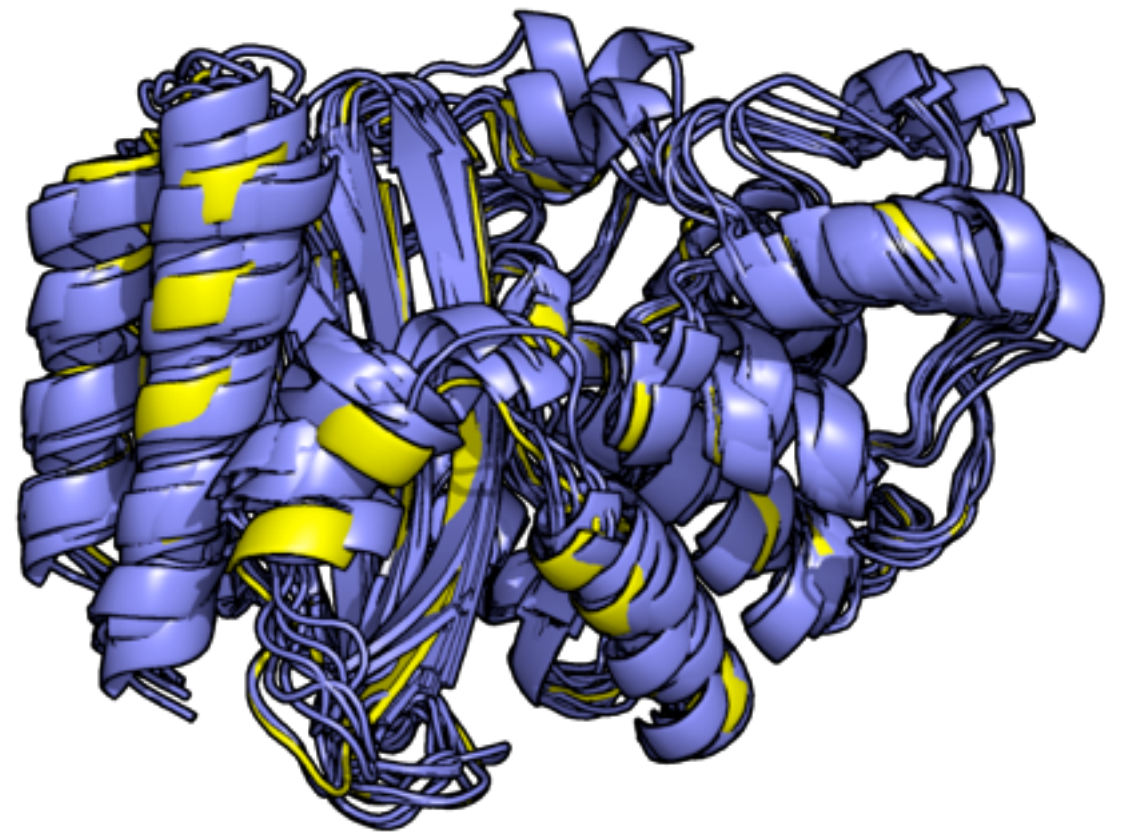
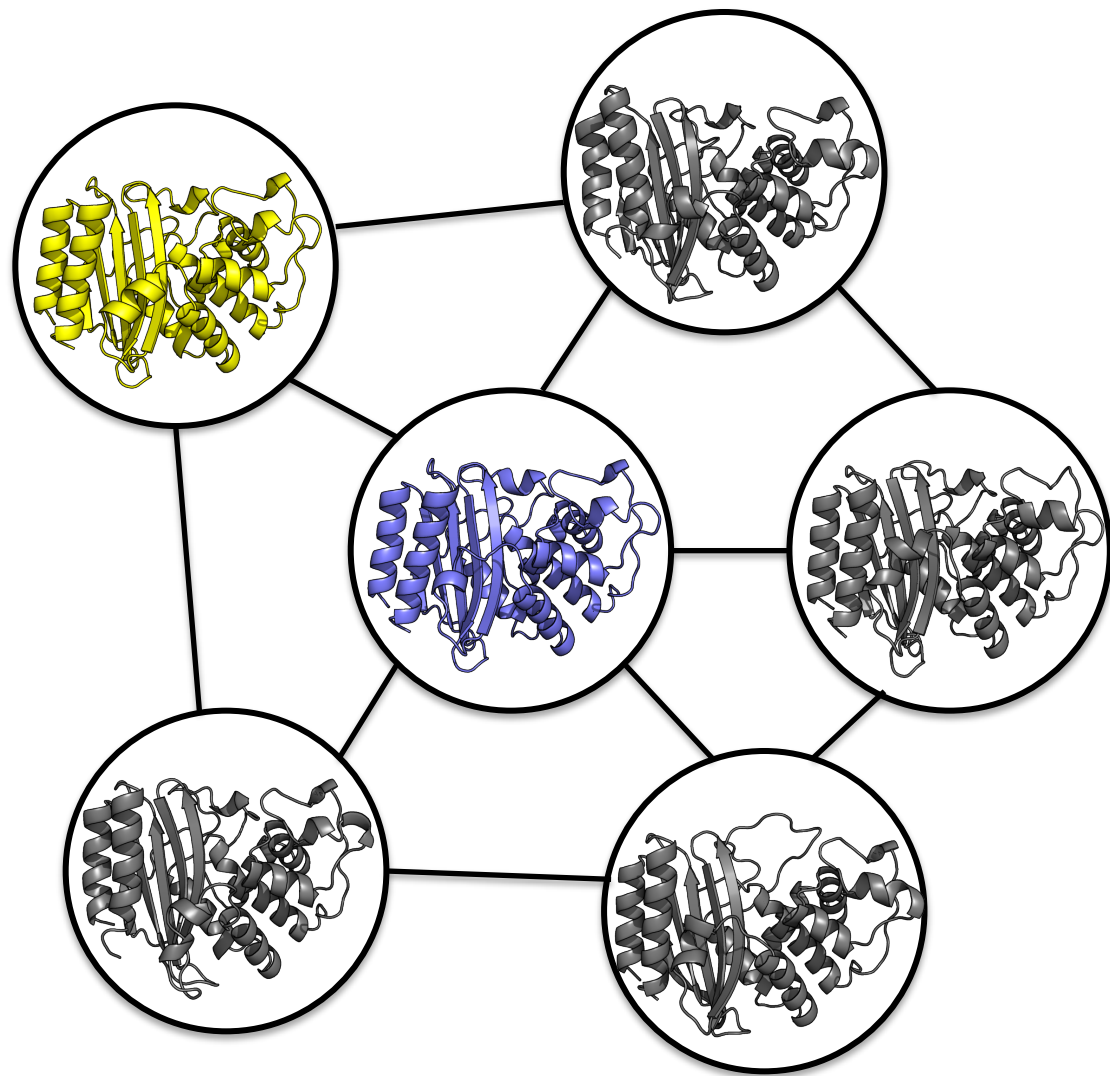
Bowman. JCP 2012.  
Bowman *et al.* Cell Res. 2010.  
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Bowman. JCP 2012.  
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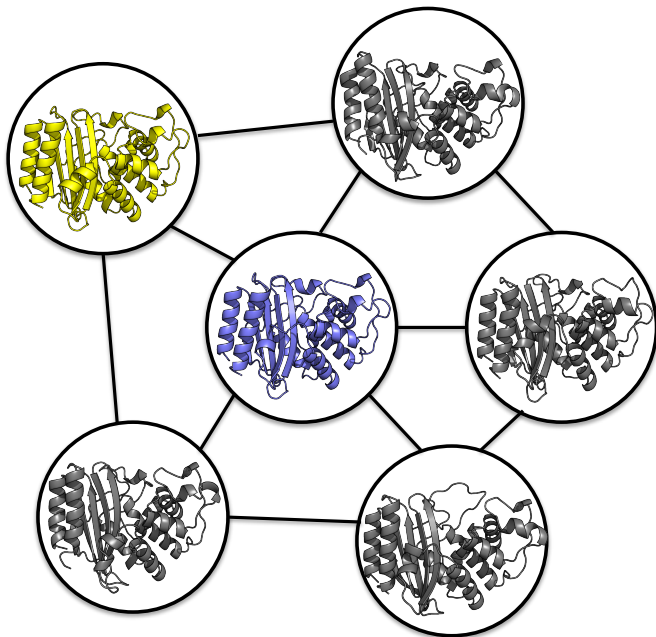
# Coarse-graining Markov models facilitates understanding



Bowman. JCP 2012.  
Bowman *et al.* Cell Res. 2010.  
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# Outline



Computational  
approach

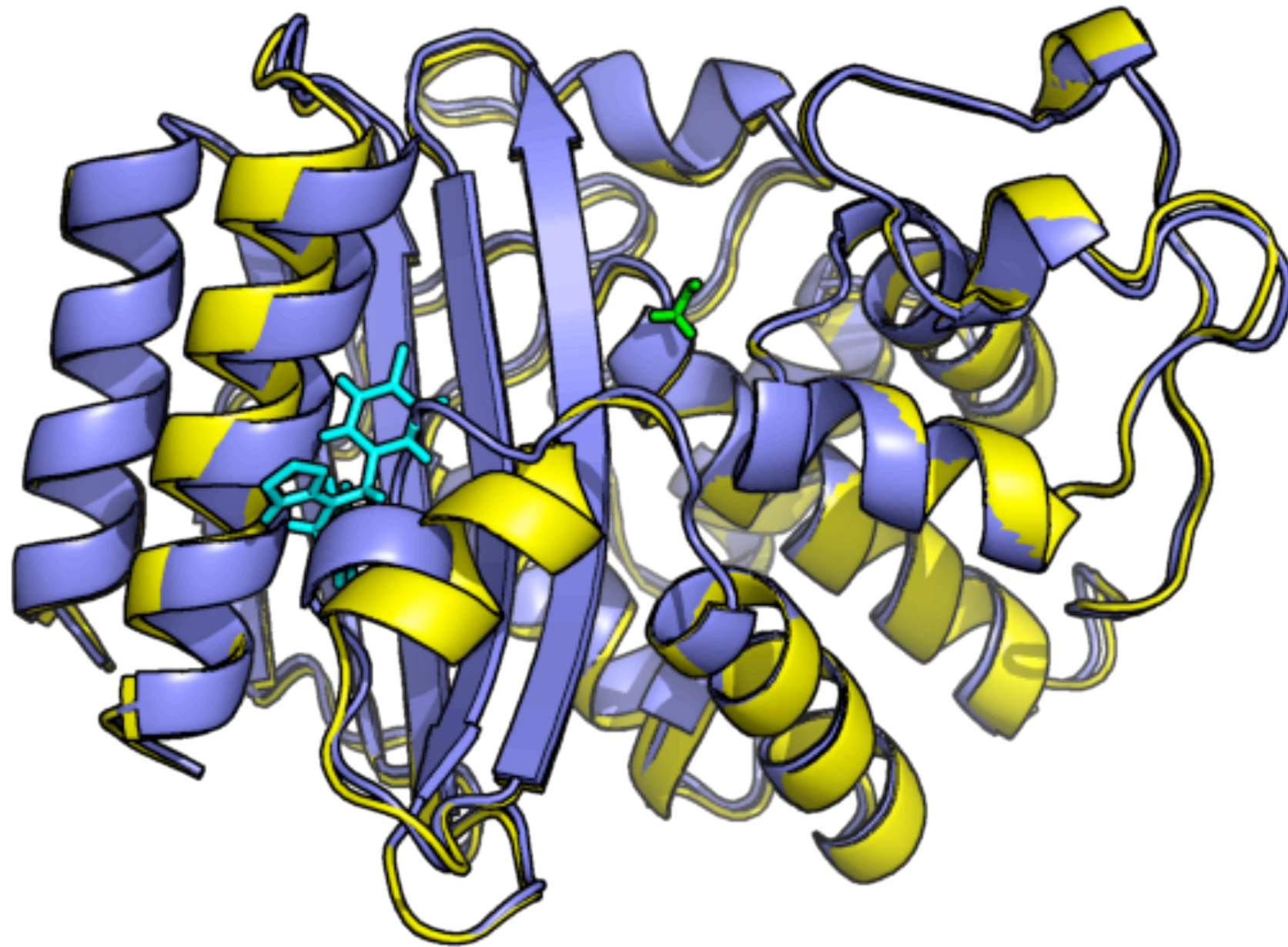
?

Understanding  
and predicting  
allostery

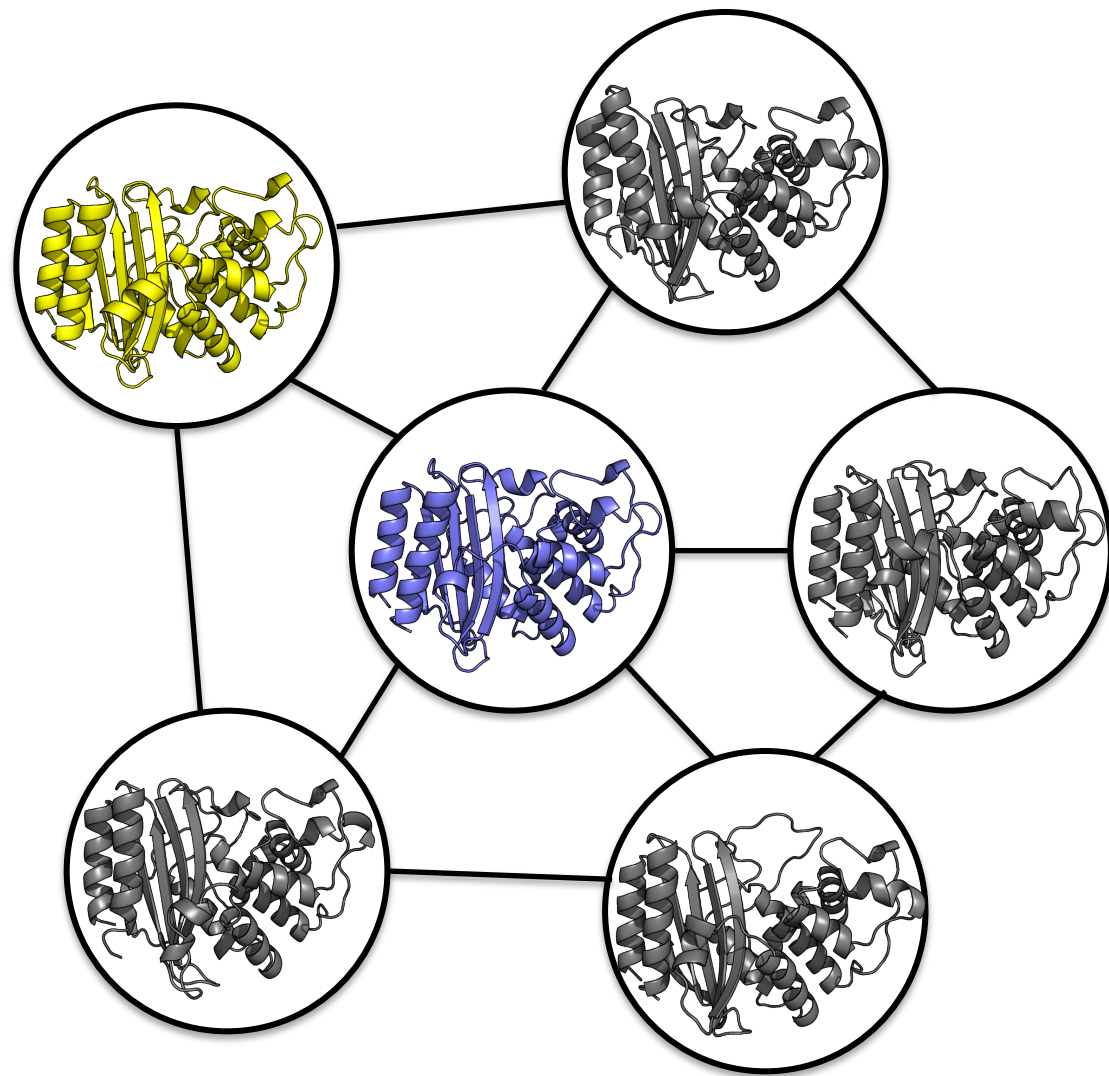
?

Experimental  
tests

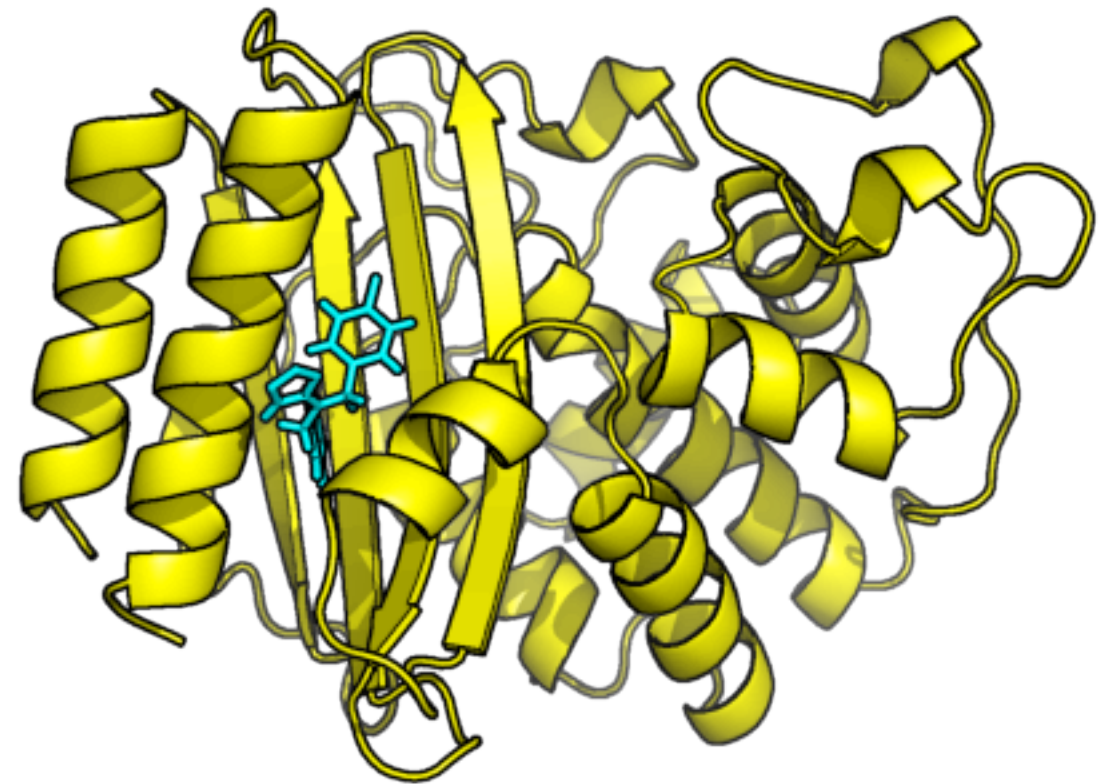
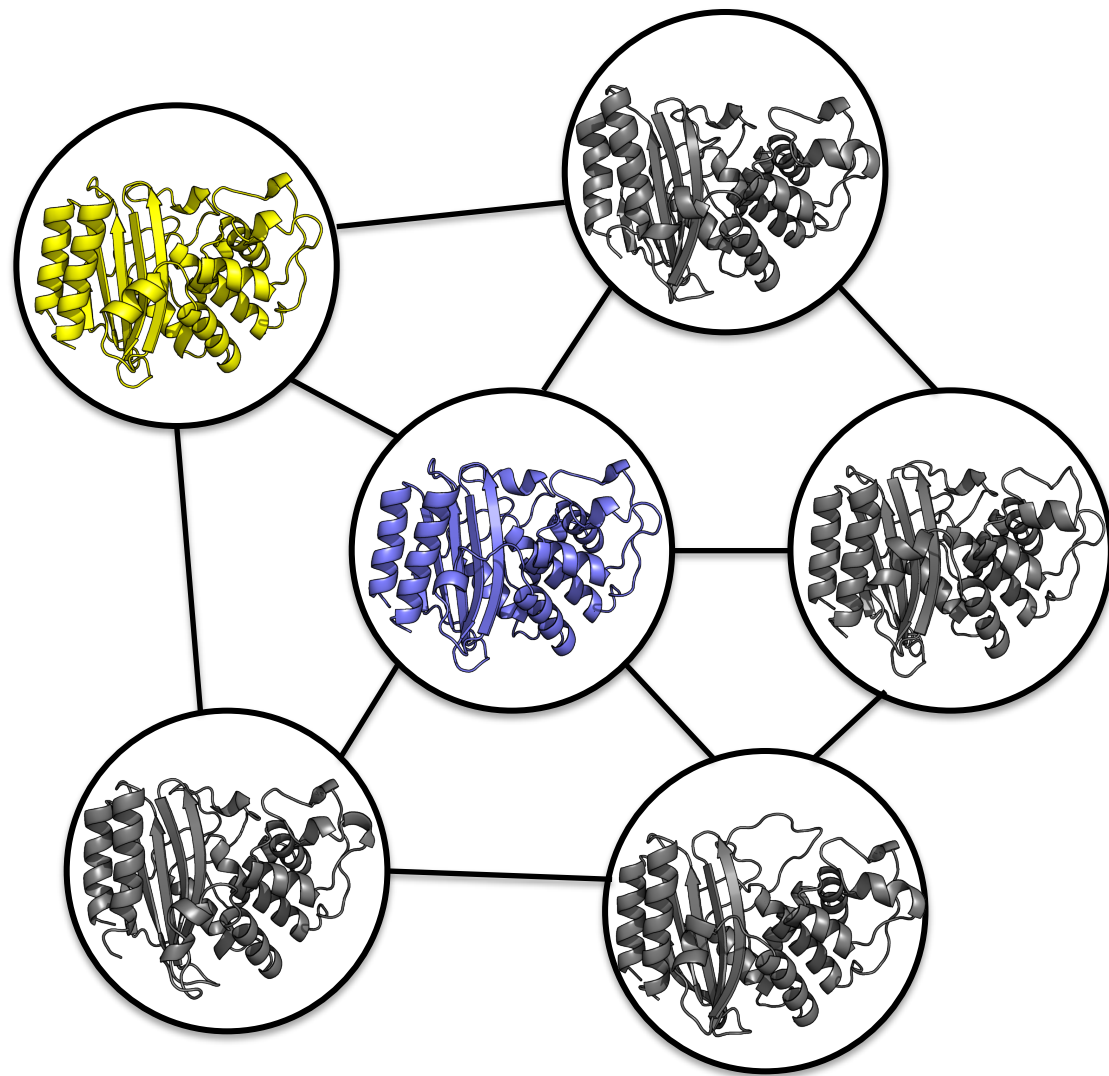
Hidden allosteric sites should be detectable on the basis of two signature structural fluctuations



# Pockets are just volumes surrounded by protein



# Pockets are just volumes surrounded by protein

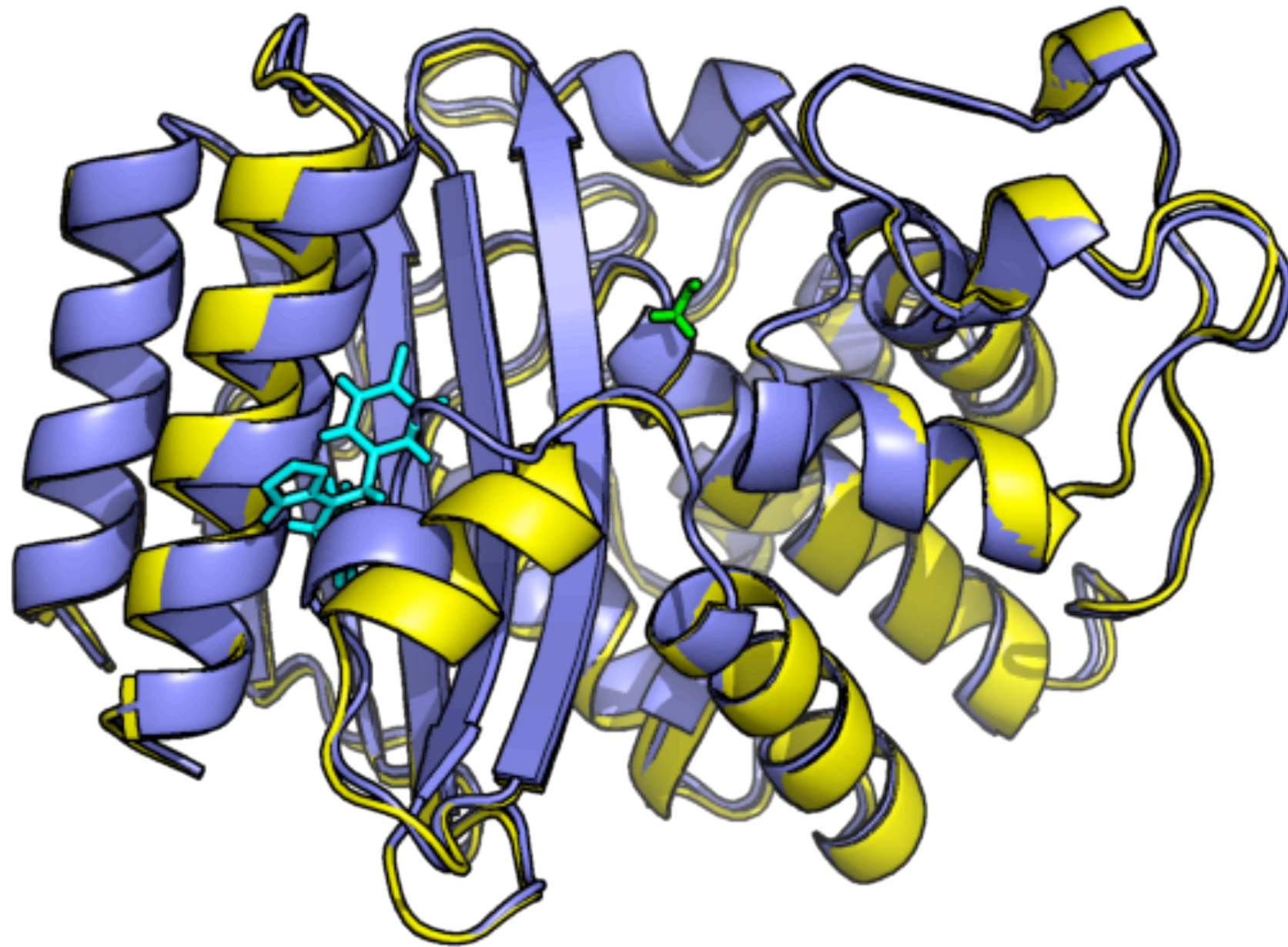


The known pocket is visible even in the  
absence of any ligand



The known pocket opens more widely  
than in the ligand-bound state

We also need some form of communication for an allosteric effect



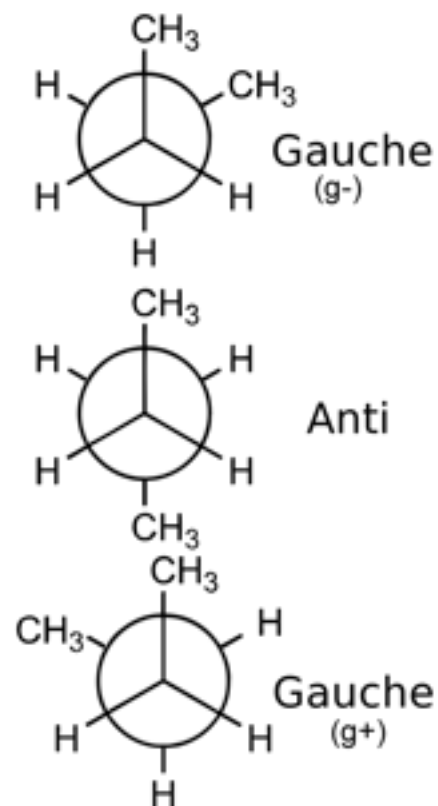
# Correlations between side-chain rotameric states allows long-distance communication

Bowman and Geissler. *PNAS* 2012.

DuBay and Geissler. *JMB* 2009.

McClendon et al. *JCTC* 2009.

# Correlations between side-chain rotameric states allows long-distance communication

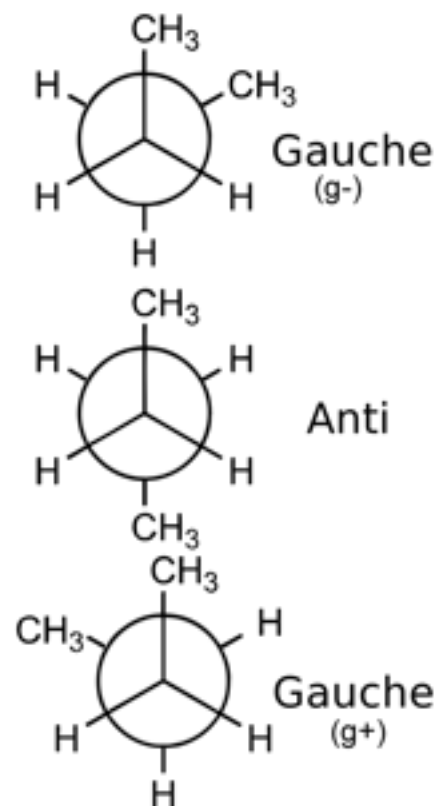


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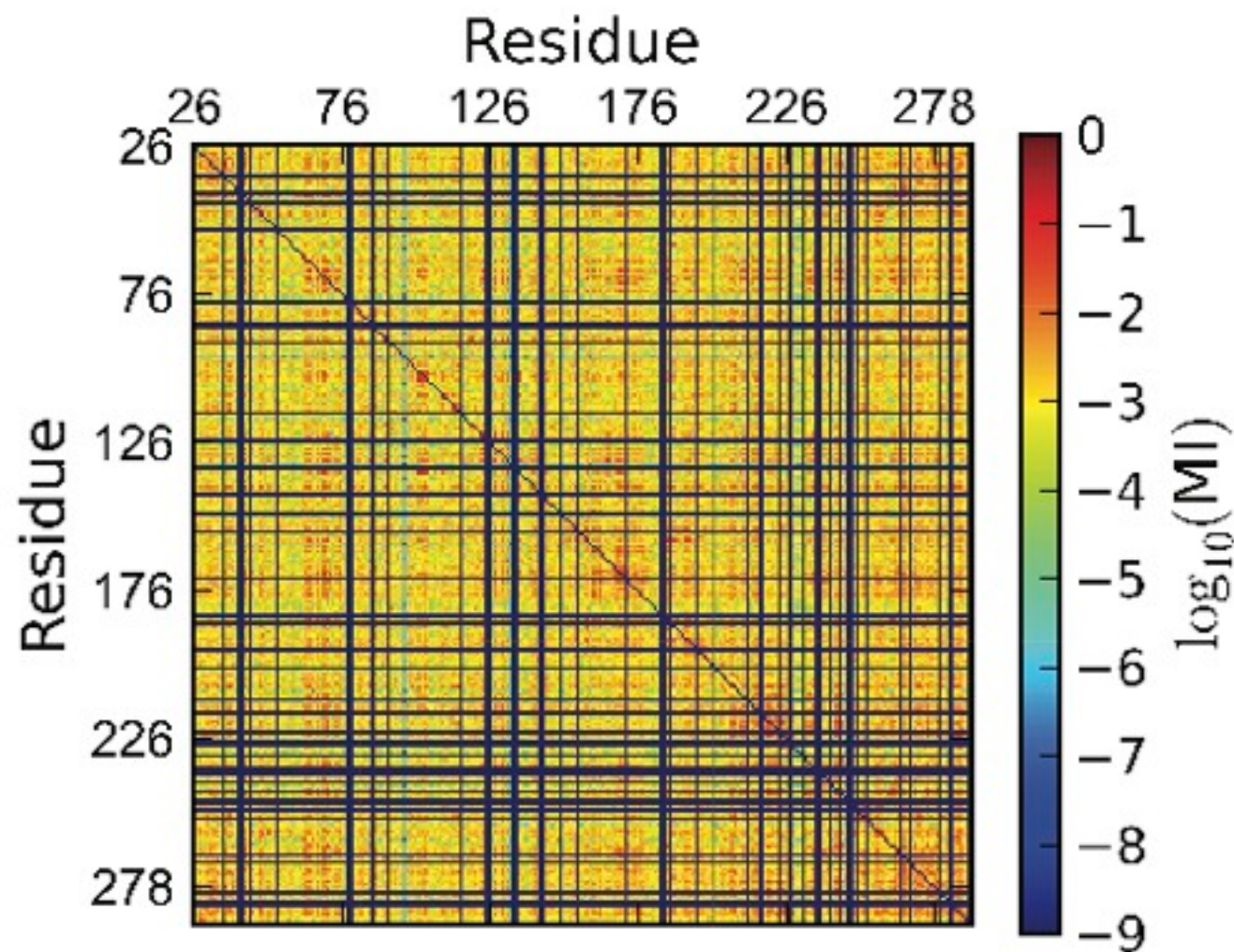
$$\text{MI}(X, Y) = \sum_{x \in x} \sum_{y \in y} p(x, y) \log \left( \frac{p(x, y)}{p(x)p(y)} \right)$$

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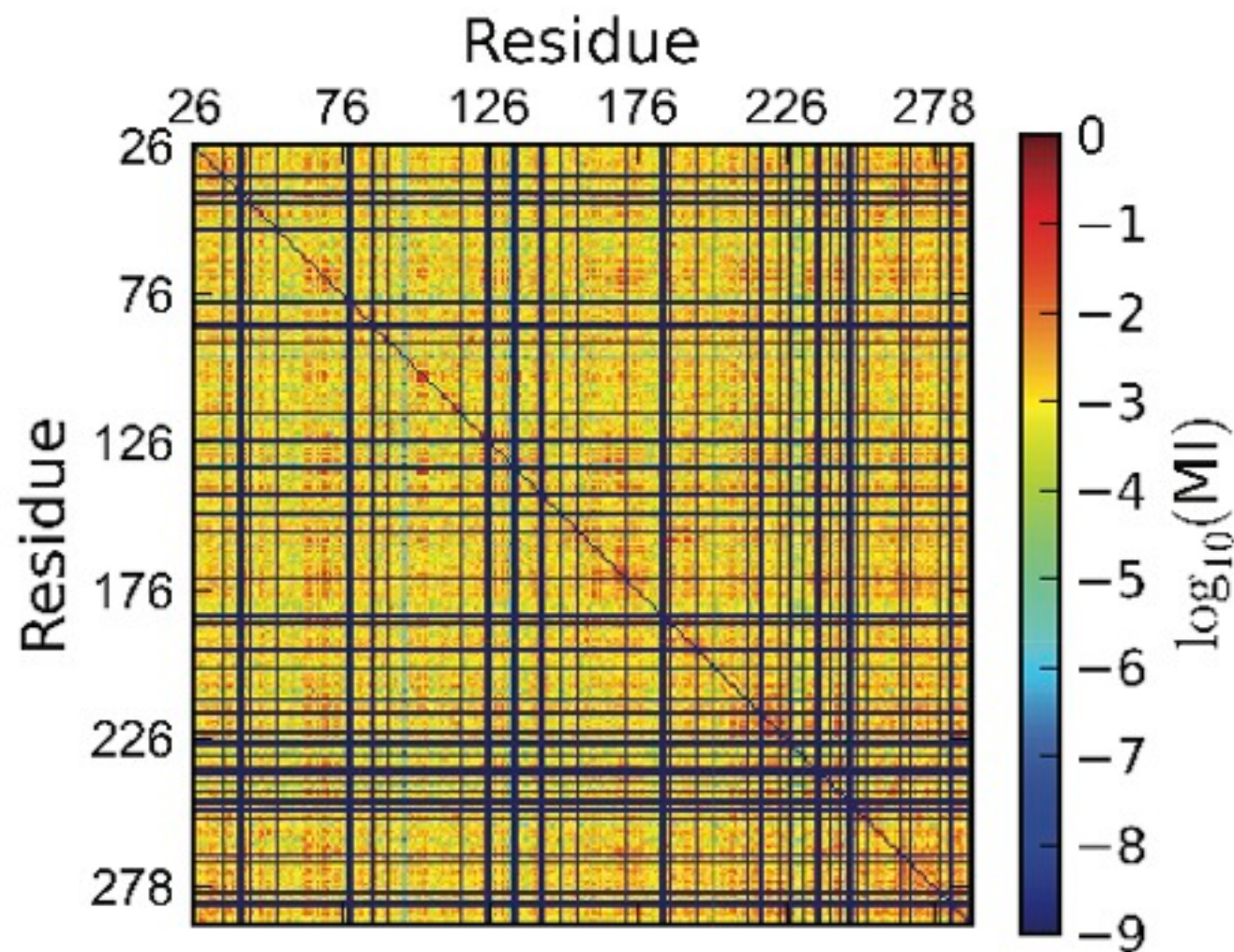
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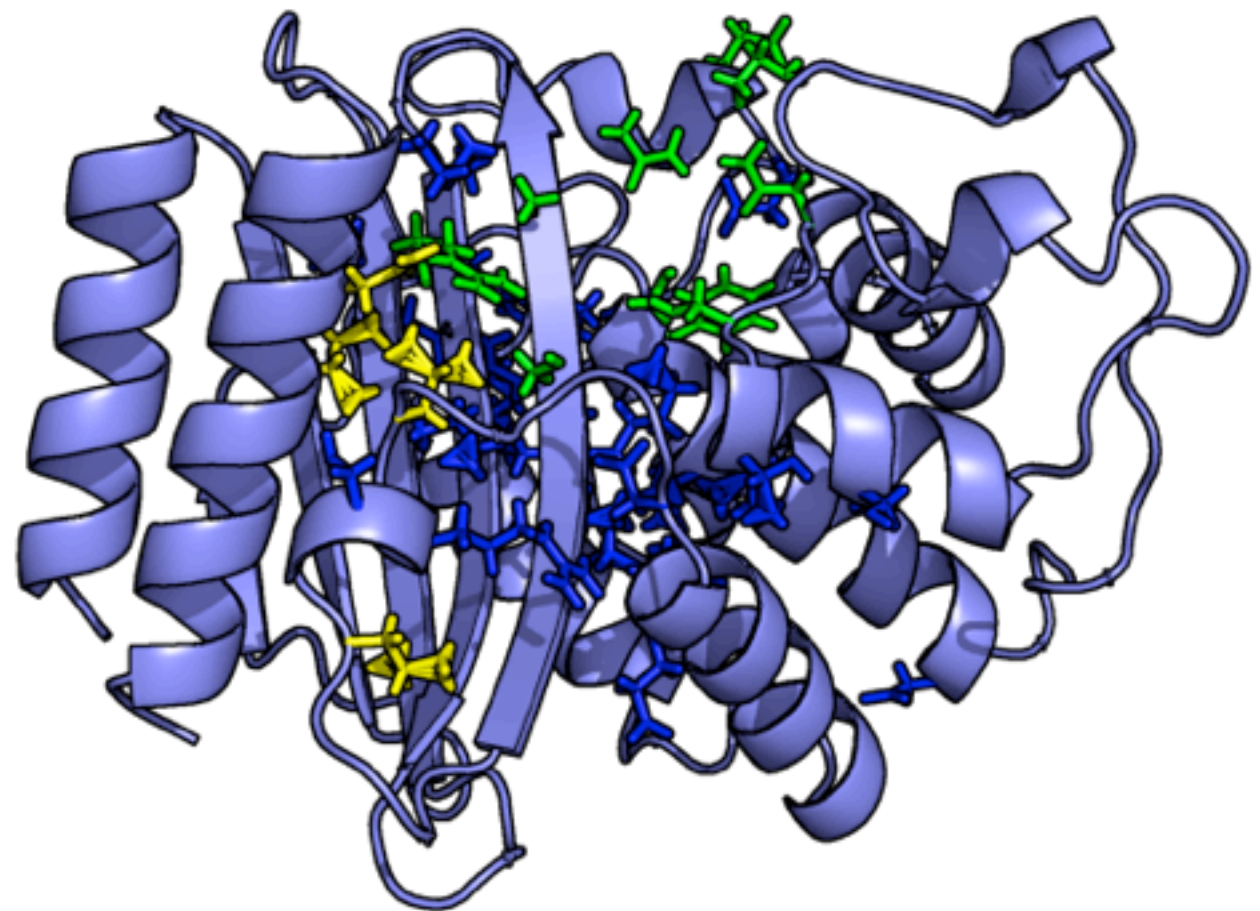
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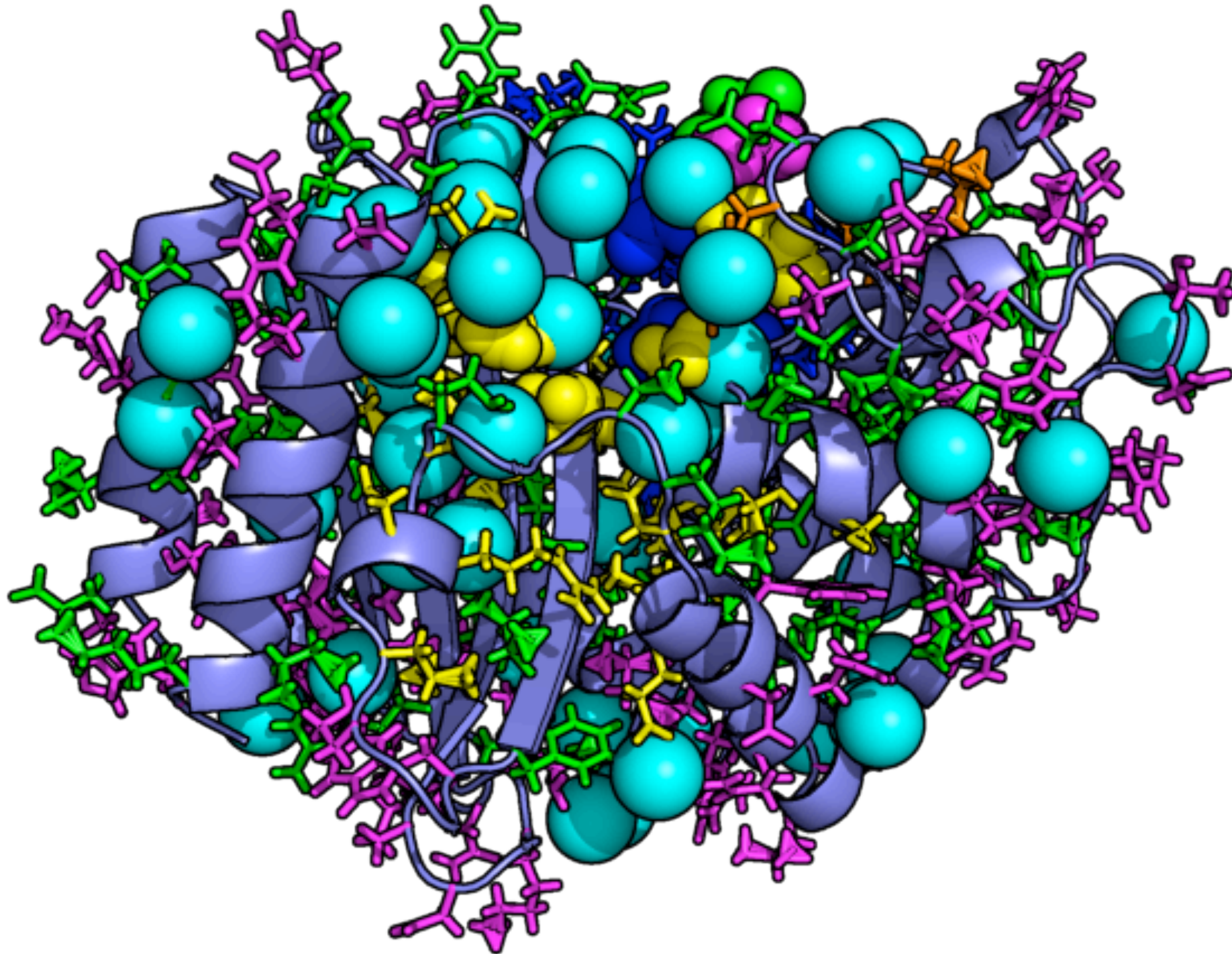
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DuBay and Geissler. *JMB* 2009.

McClendon et al. *JCTC* 2009.

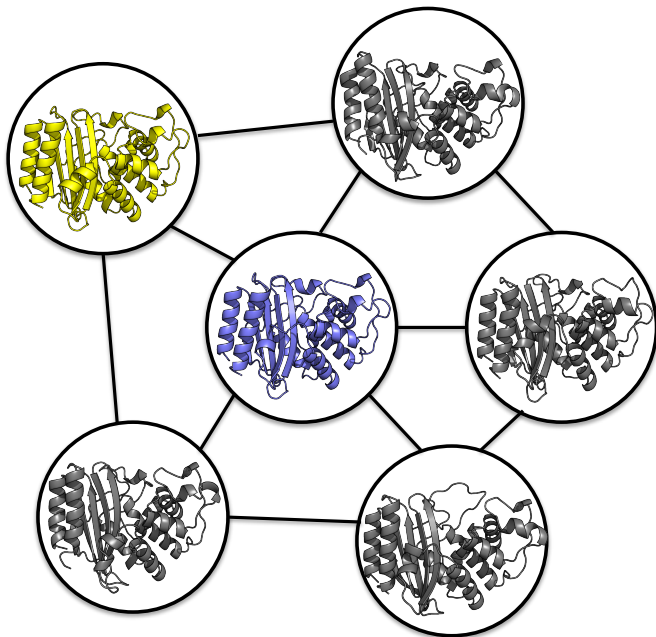


There are many other potential cryptic  
allosteric sites

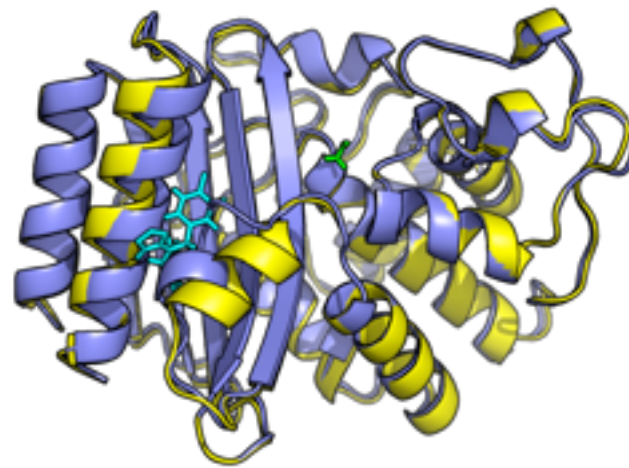




# Outline



Computational  
approach



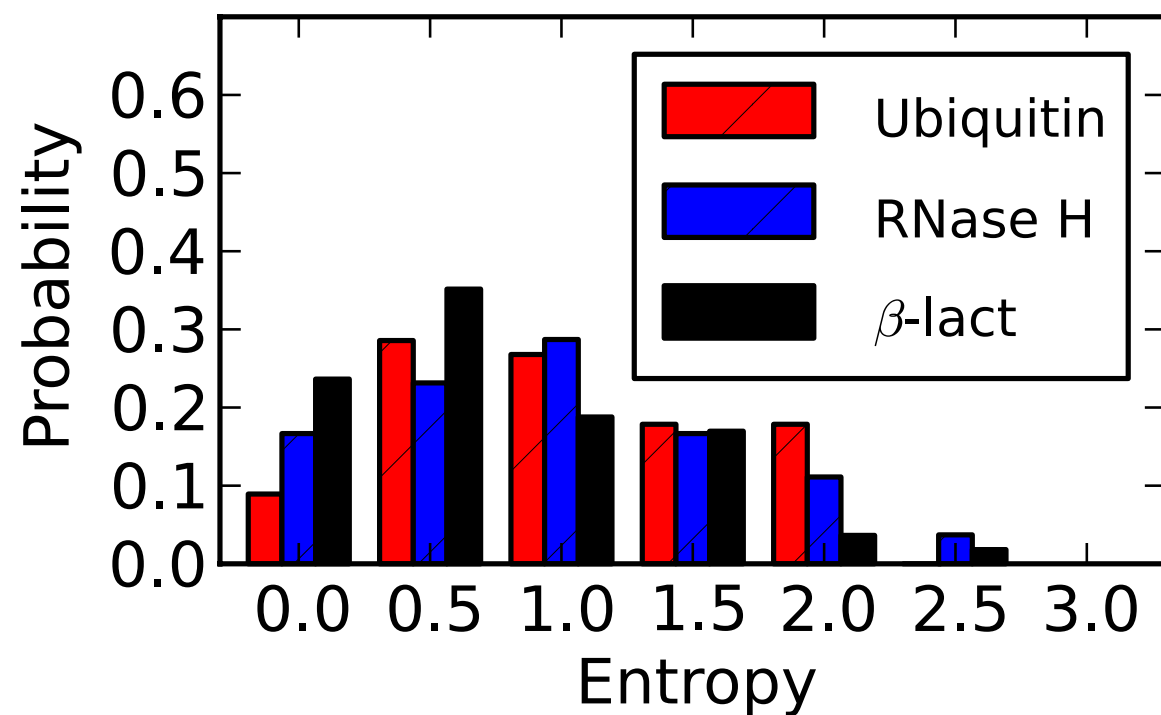
Understanding  
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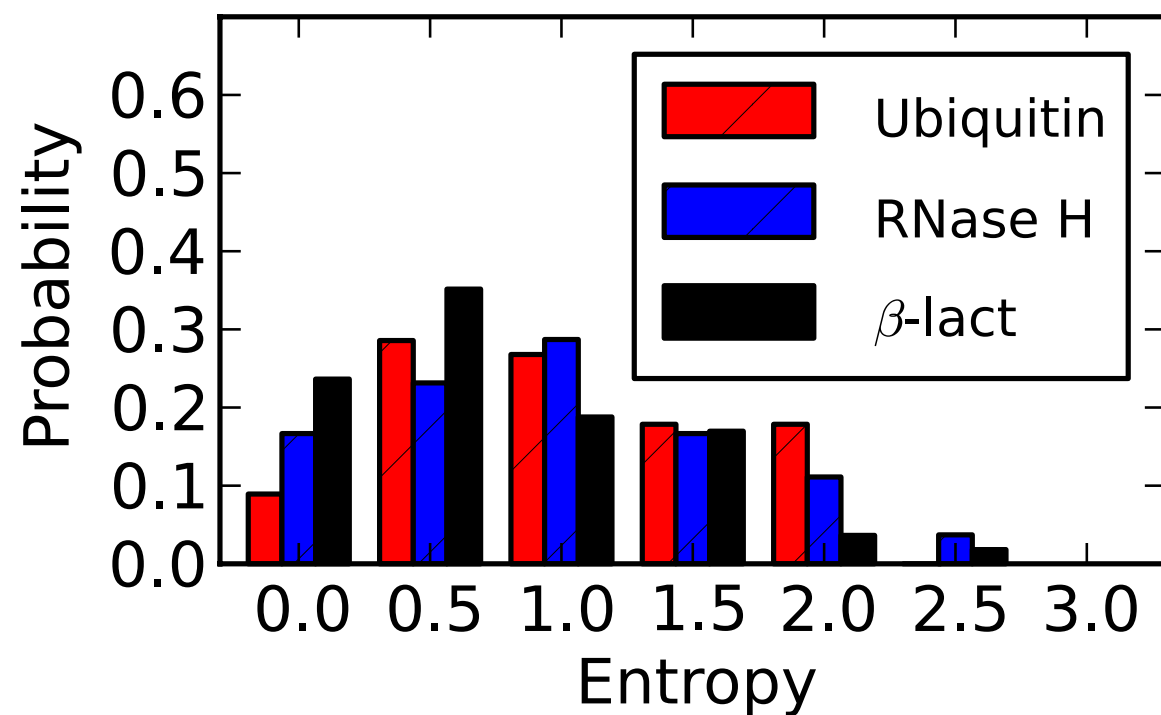
# My models predict extensive side-chain heterogeneity even in proteins' cores

## Surface

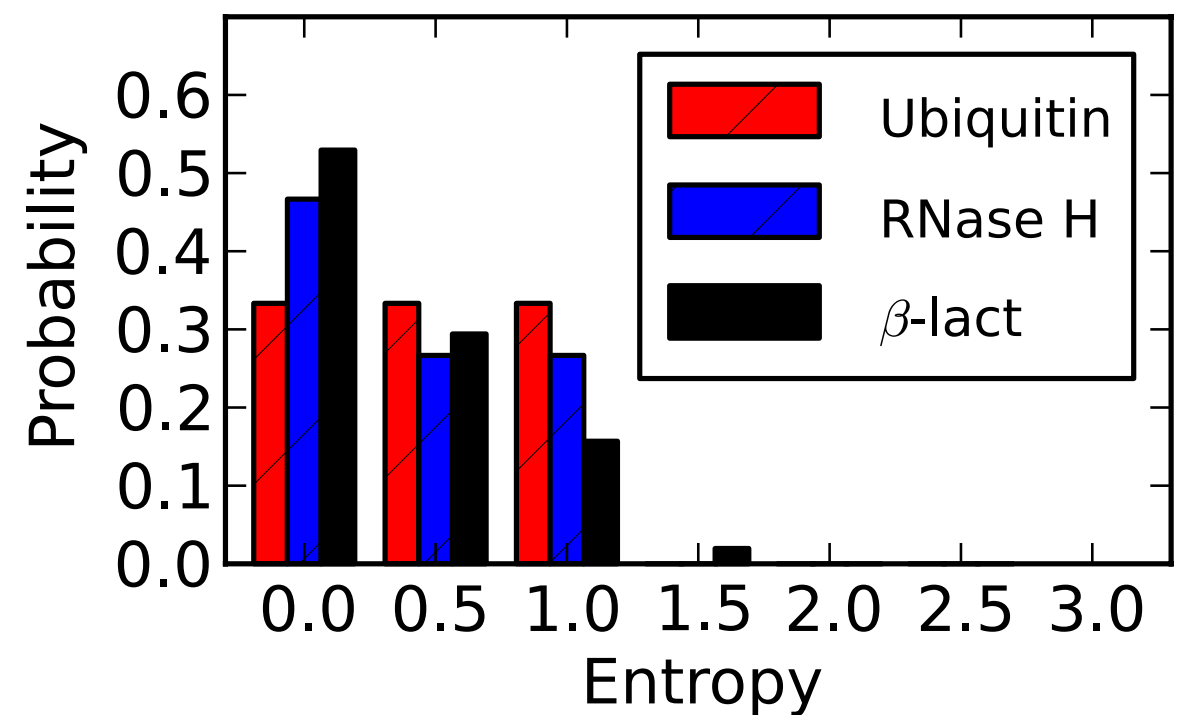


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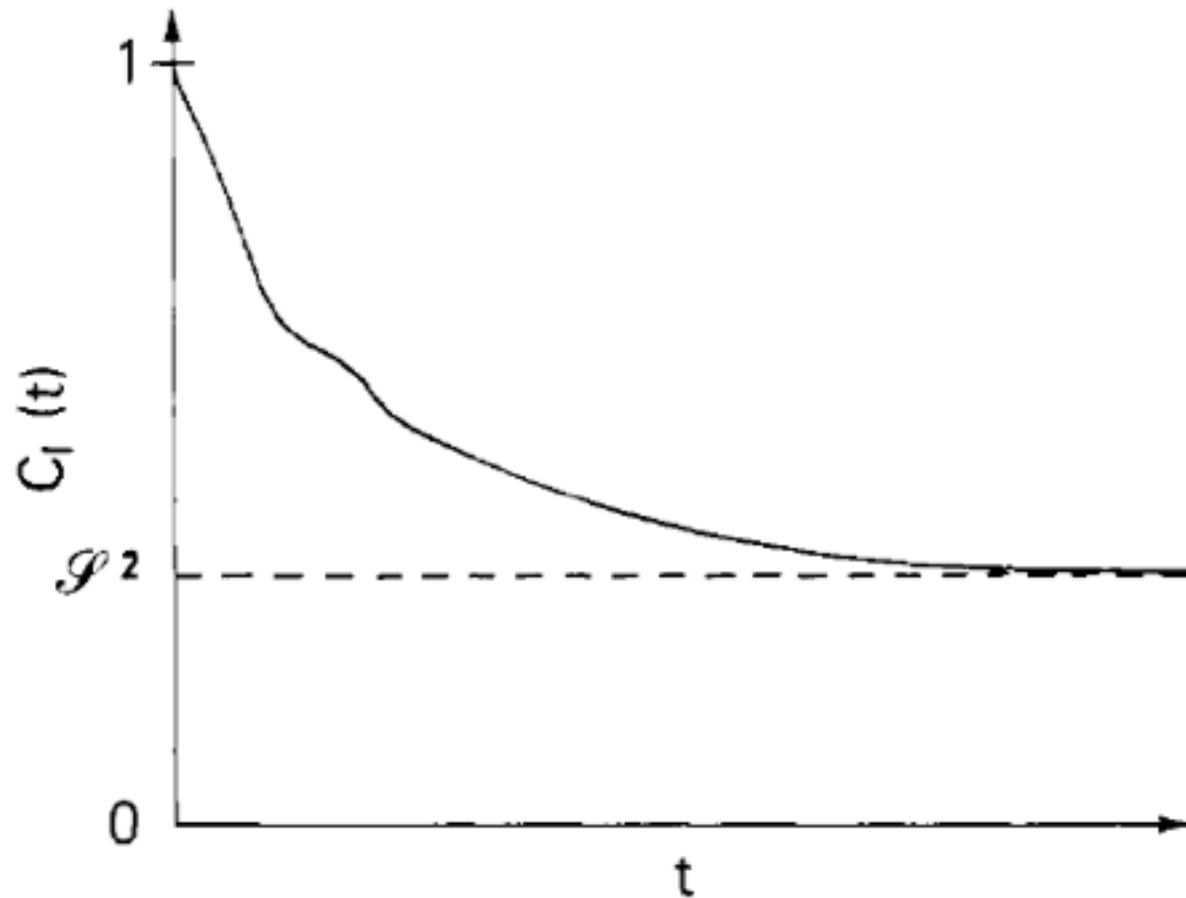
## Surface



## Core

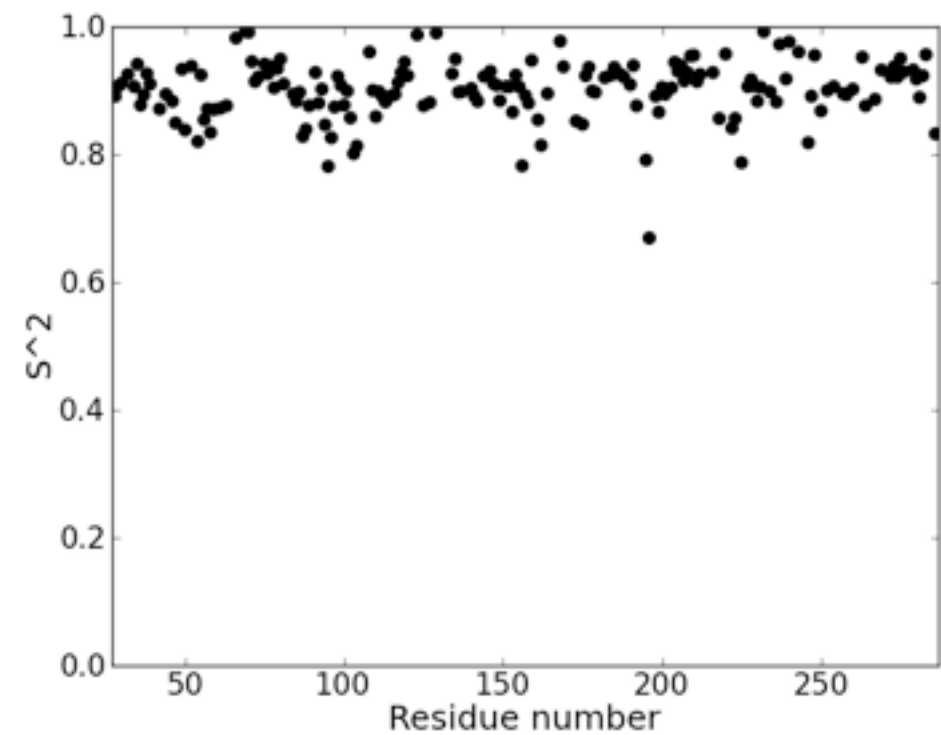
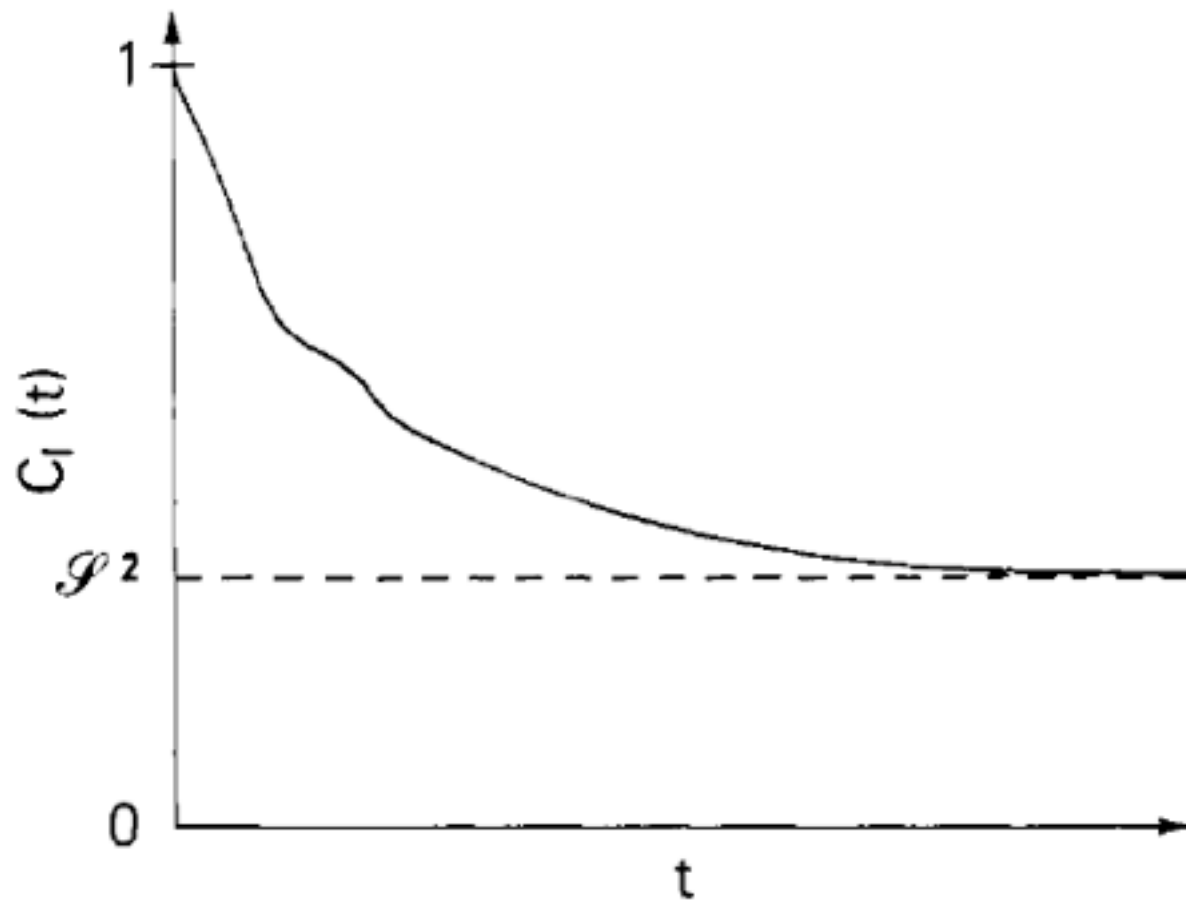


My observations are consistent with  
NMR order parameters



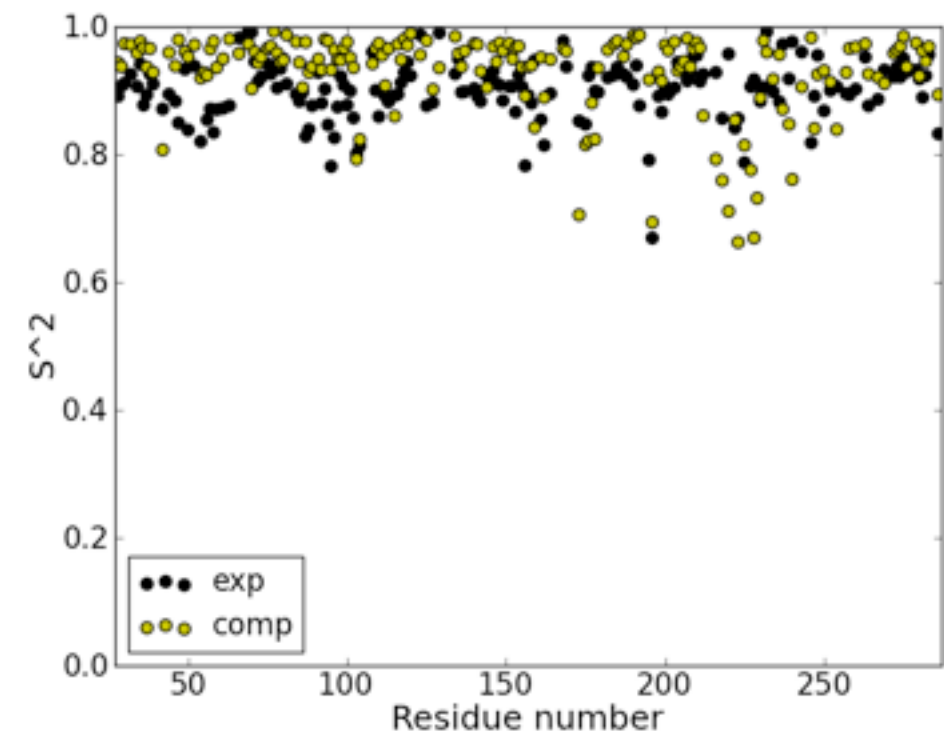
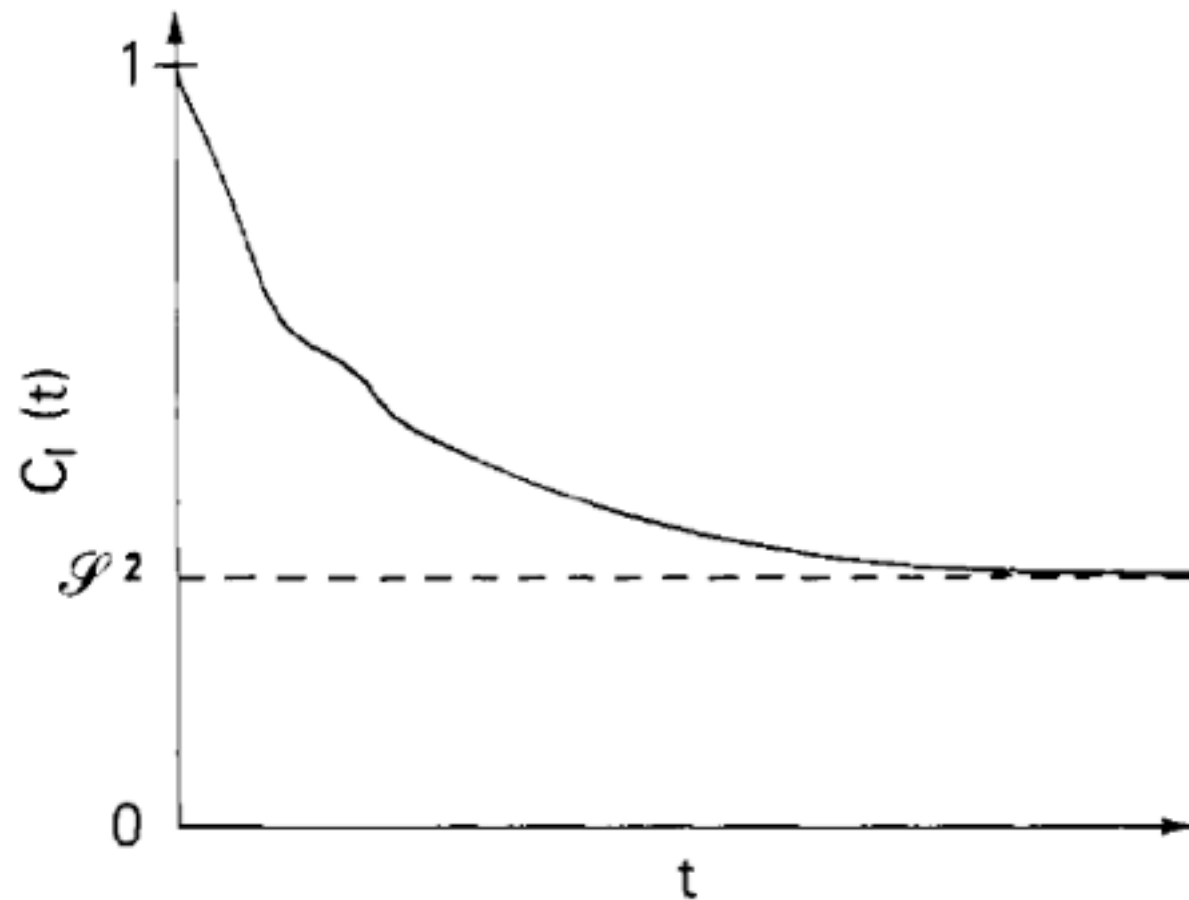
$$C_I(t) = \langle P_2(\hat{\mu}(0) \cdot \hat{\mu}(t)) \rangle$$

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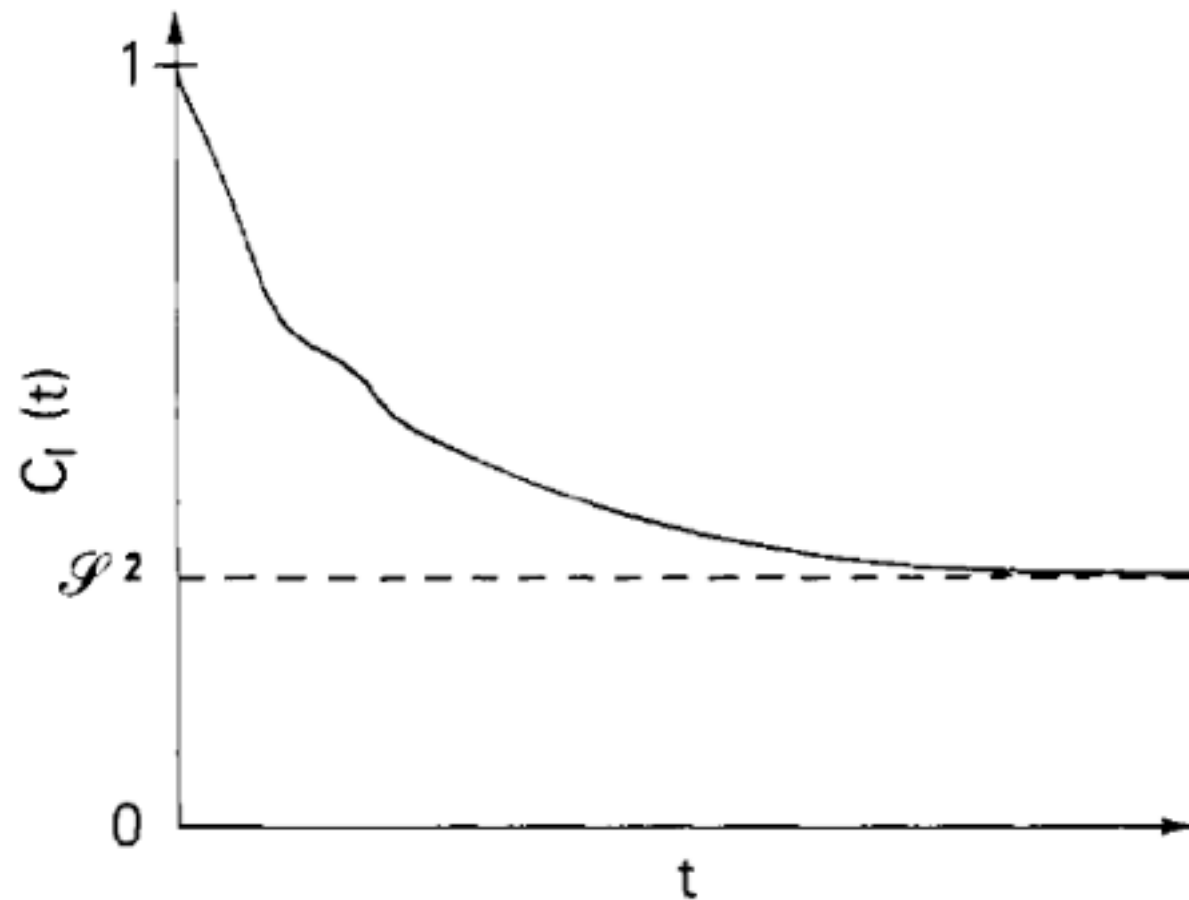
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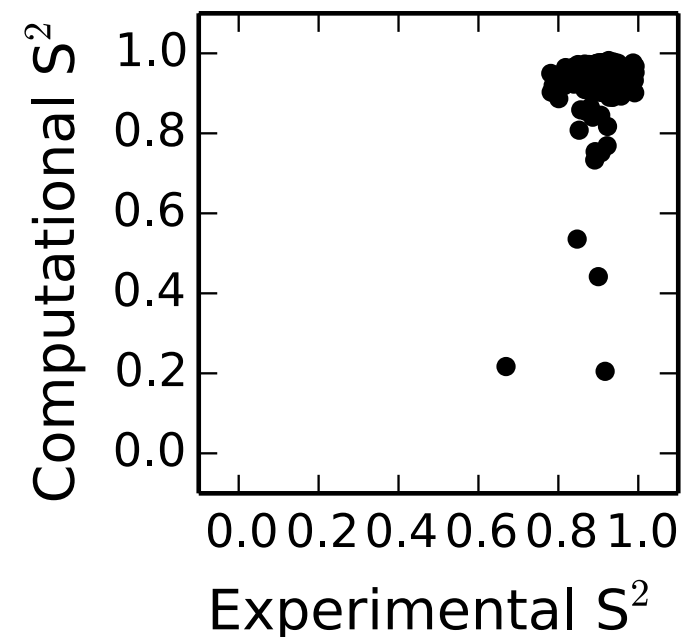
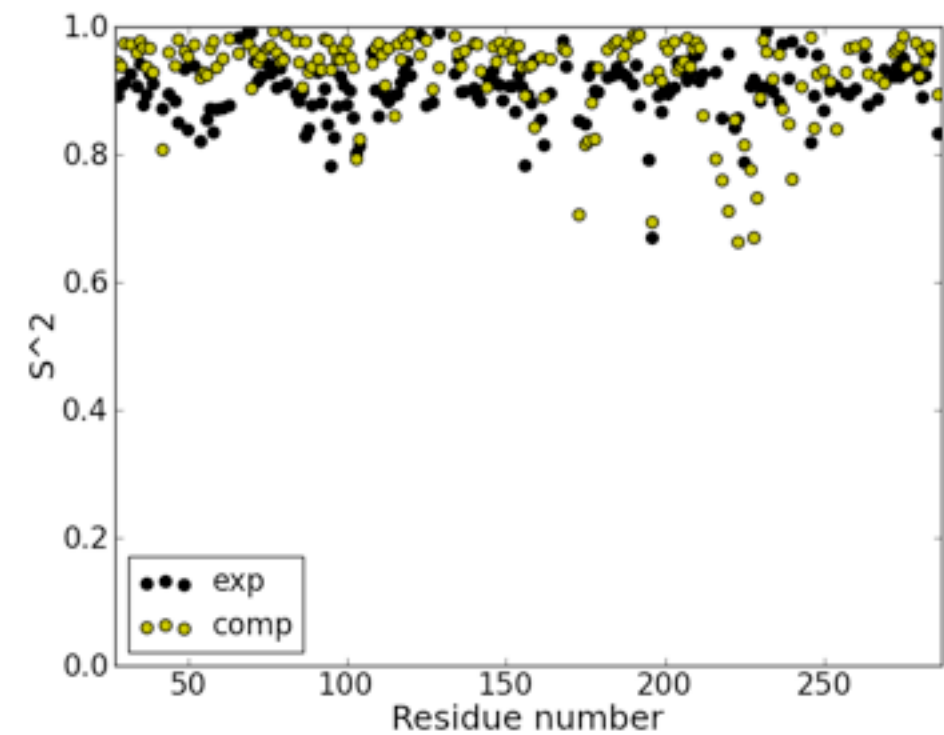


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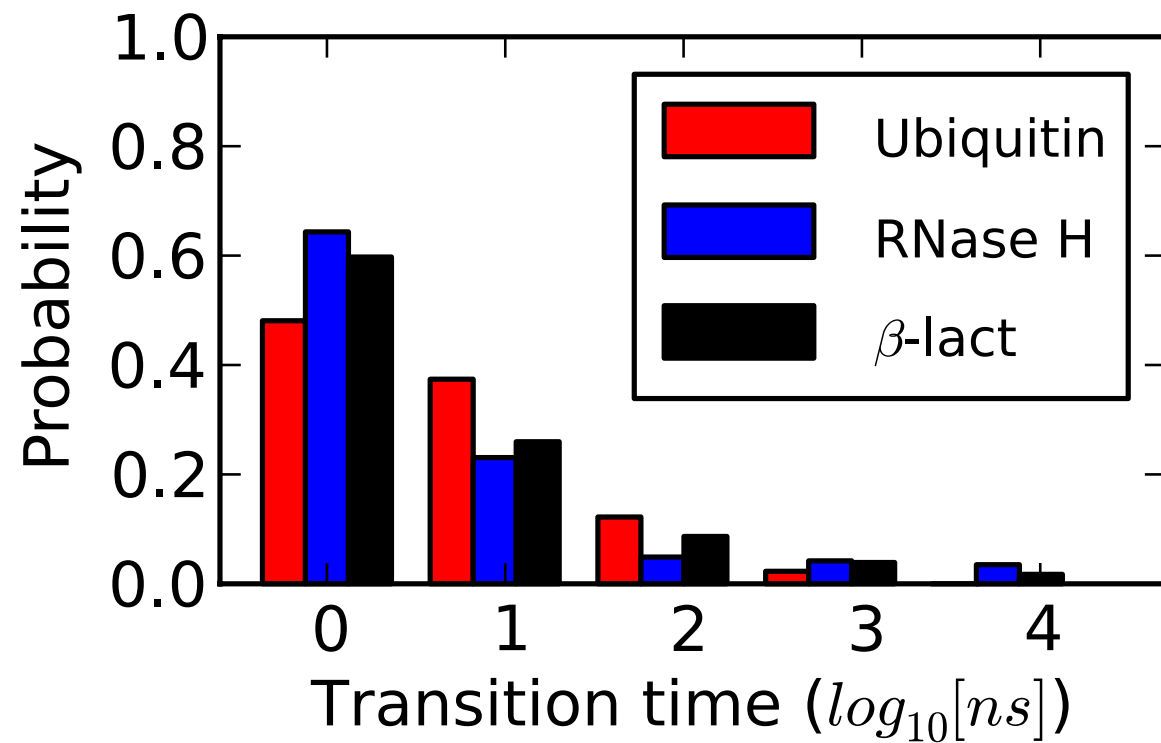


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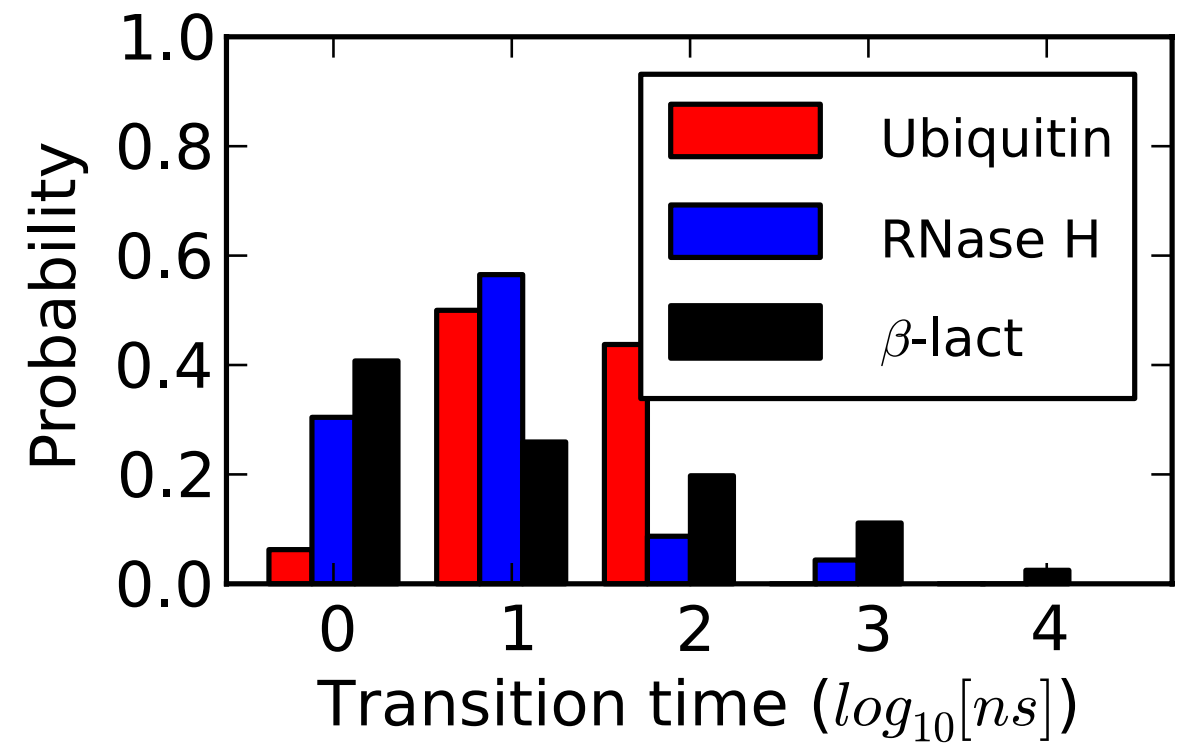


# My models provide access to the timescales for side-chain dynamics

## Surface



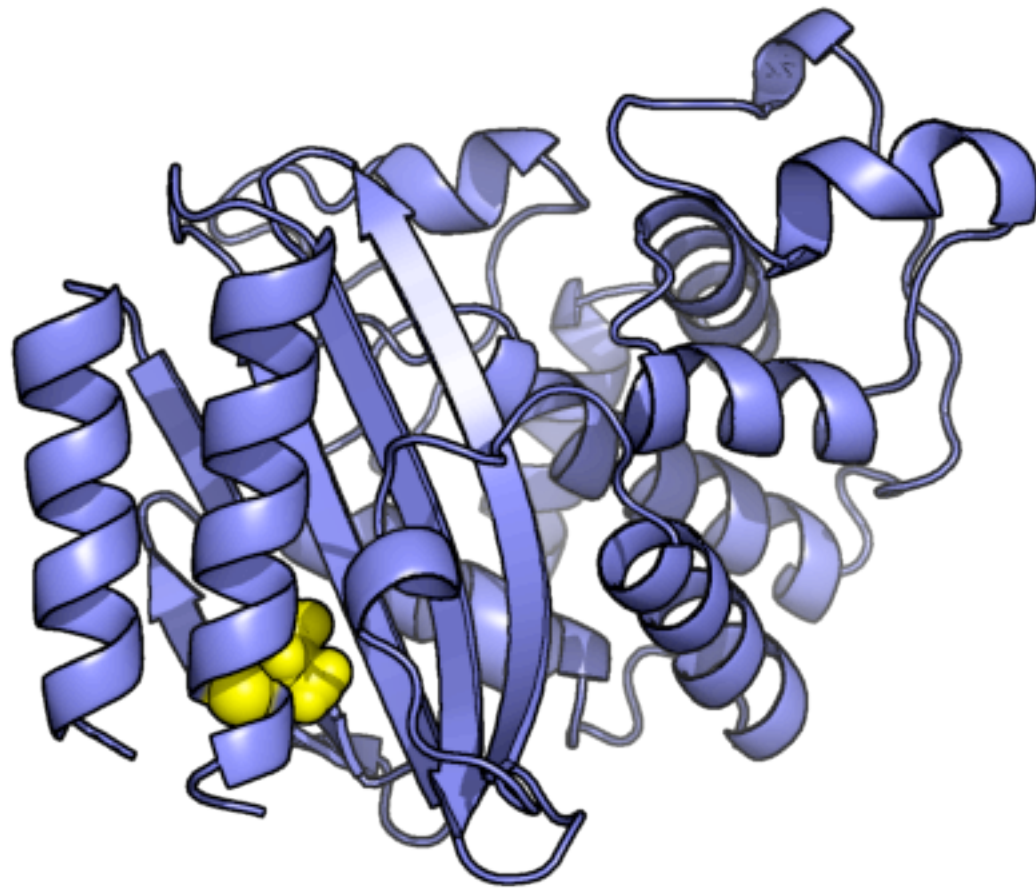
## Core



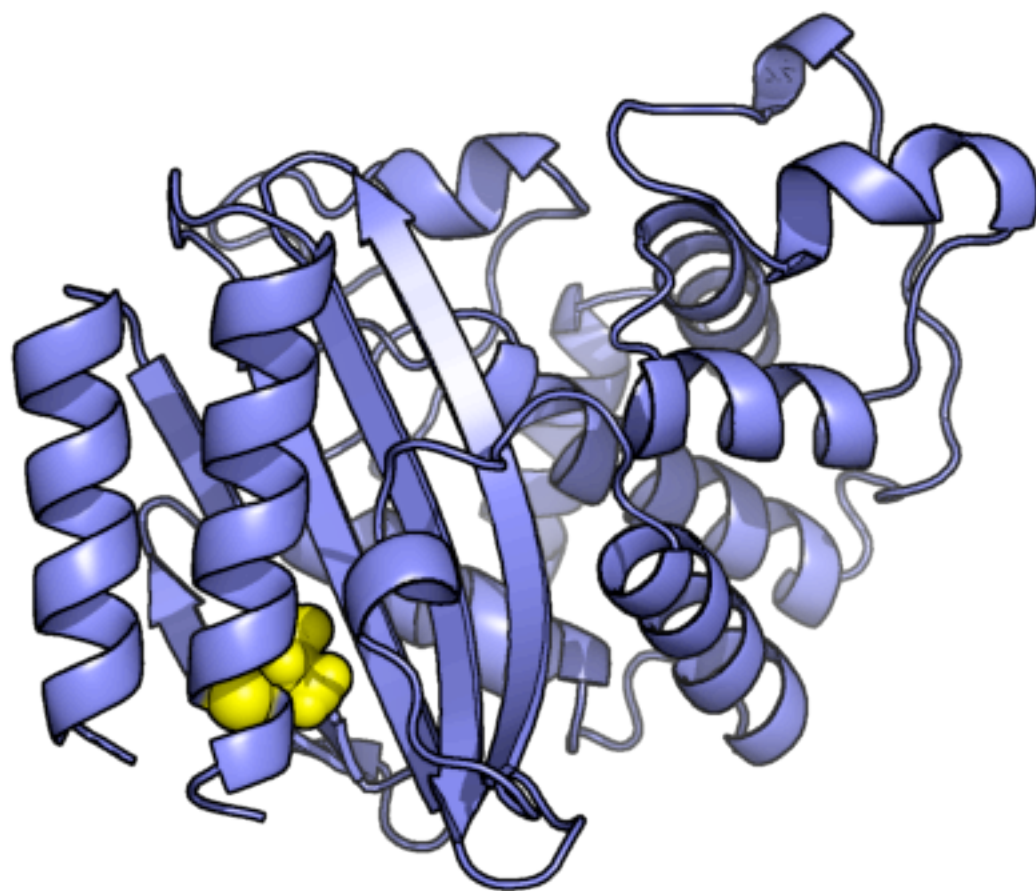


Native state thiol-exchange provides a  
direct test of my predicted pockets

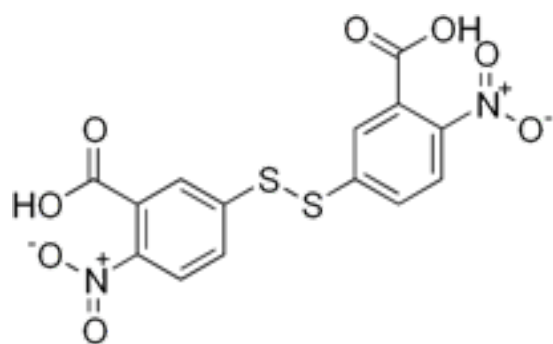
Native state thiol-exchange provides a  
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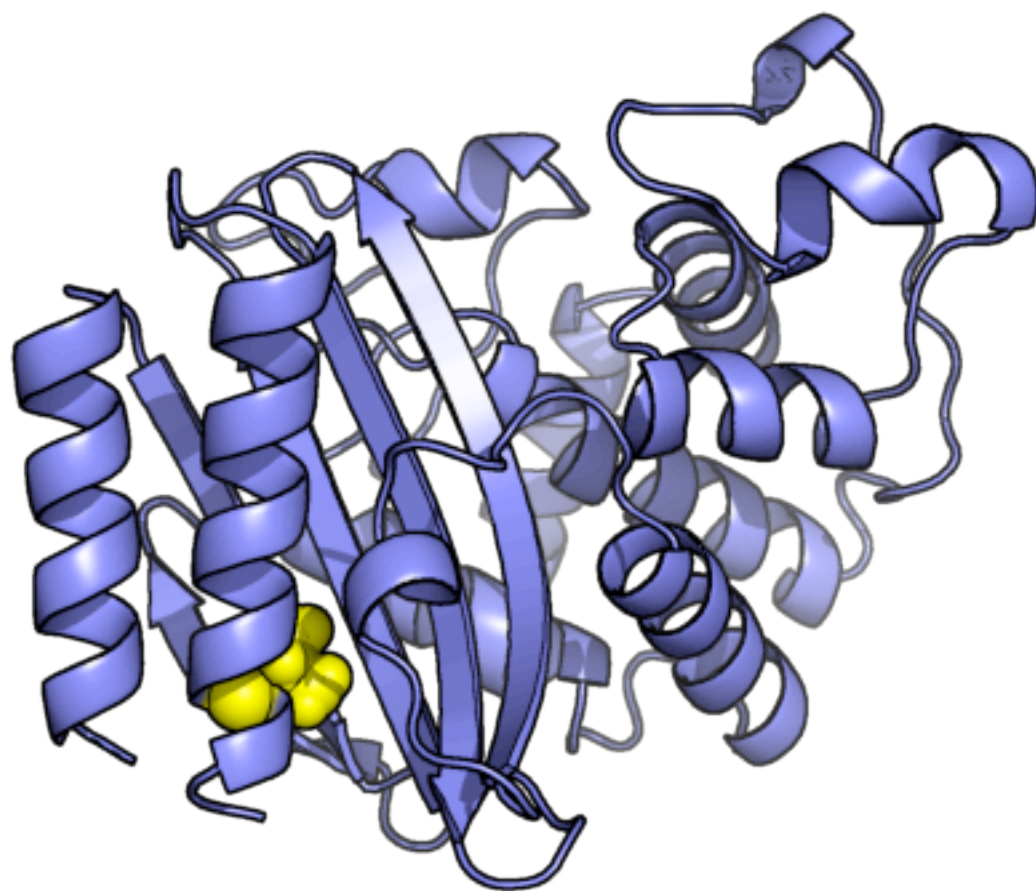
Native state thiol-exchange provides a direct test of my predicted pockets



DTNB

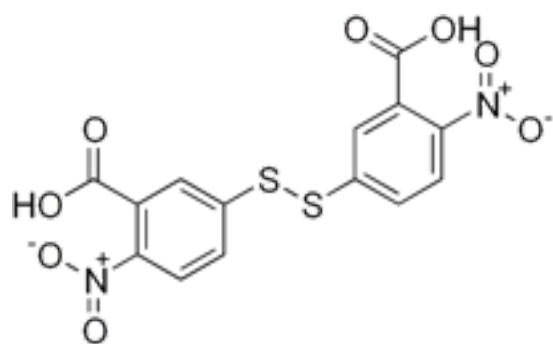


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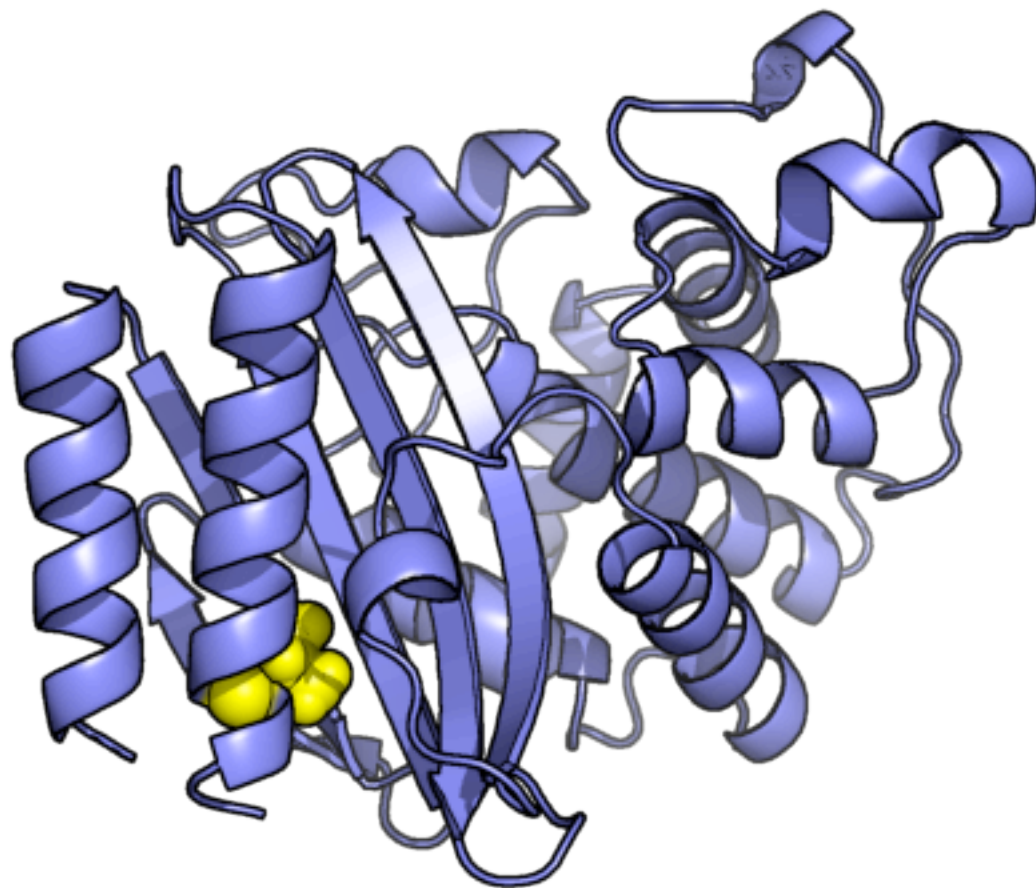


Closed  $\rightleftharpoons$  Open  $\rightarrow$  Labeled

DTNB



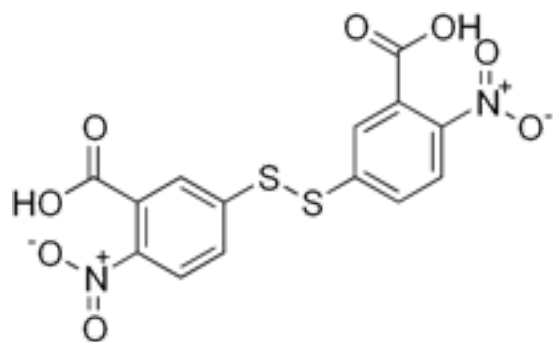
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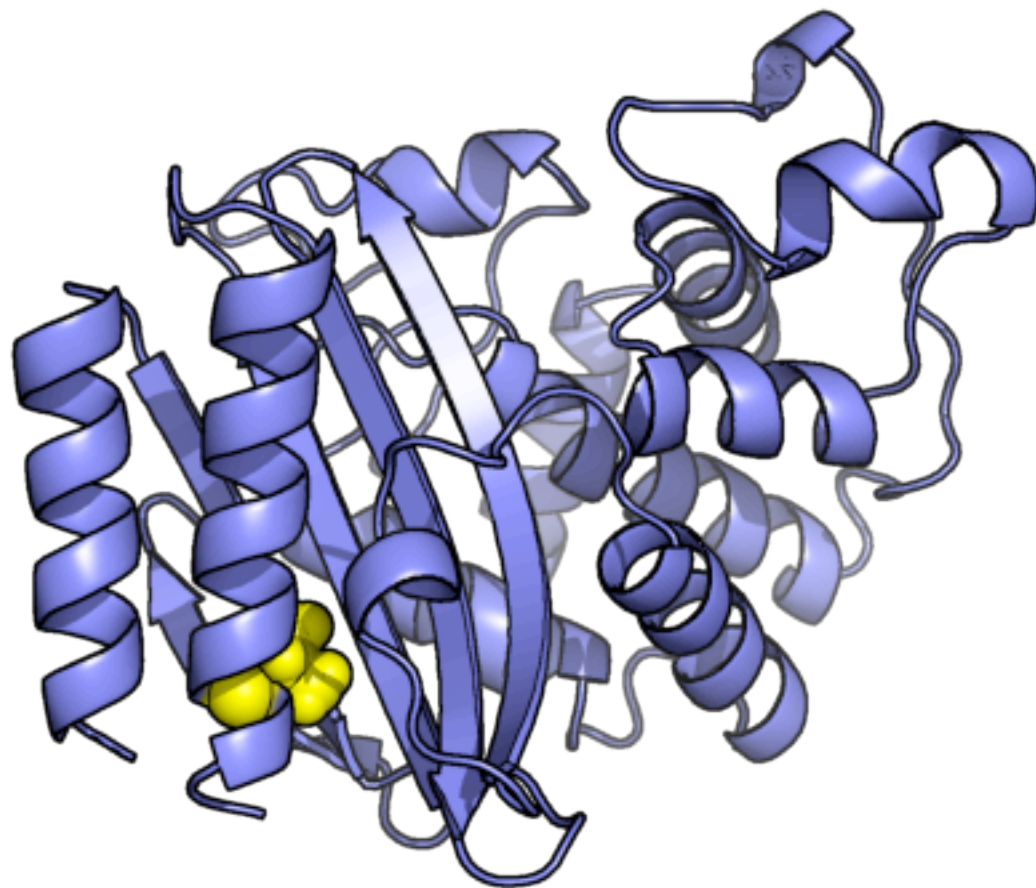
$$k_{obs} = \frac{k_{op} \times k_{int}}{k_{op} + k_{cl} + k_{int}}$$

DTNB





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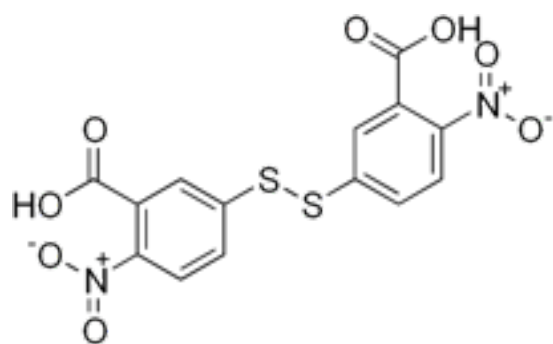
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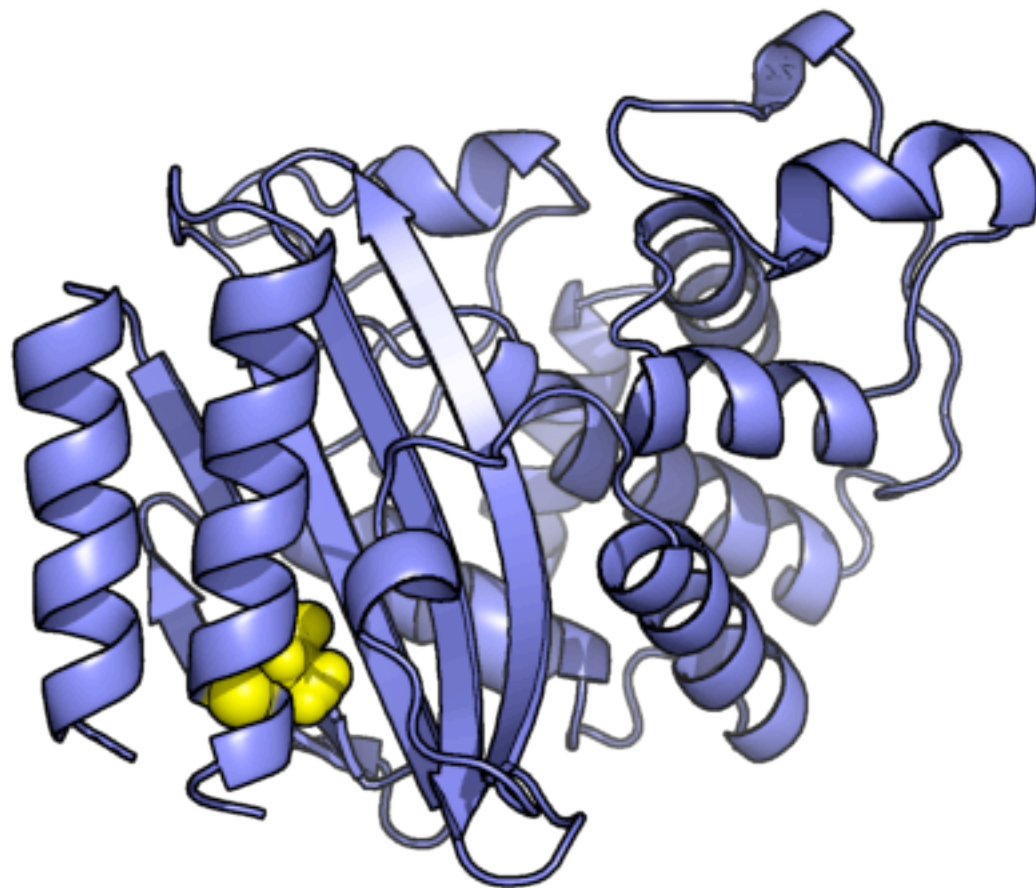
$$EX1 : k_{cl} \ll k_{int}$$

$$k_{obs} = k_{op}$$

DTNB



# Native state thiol-exchange provides a direct test of my predicted pockets



Closed  $\rightleftharpoons$  Open  $\rightarrow$  Labeled

$$k_{obs} = \frac{k_{op} \times k_{int}}{k_{op} + k_{cl} + k_{int}}$$

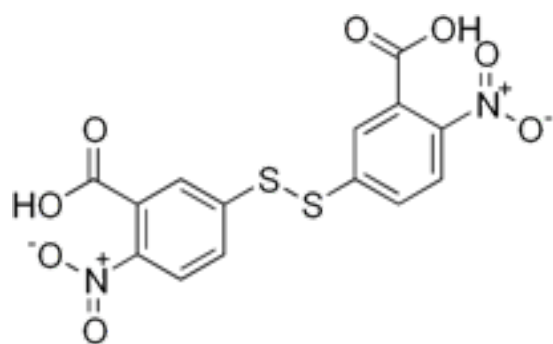
$$EX1 : k_{cl} \ll k_{int}$$

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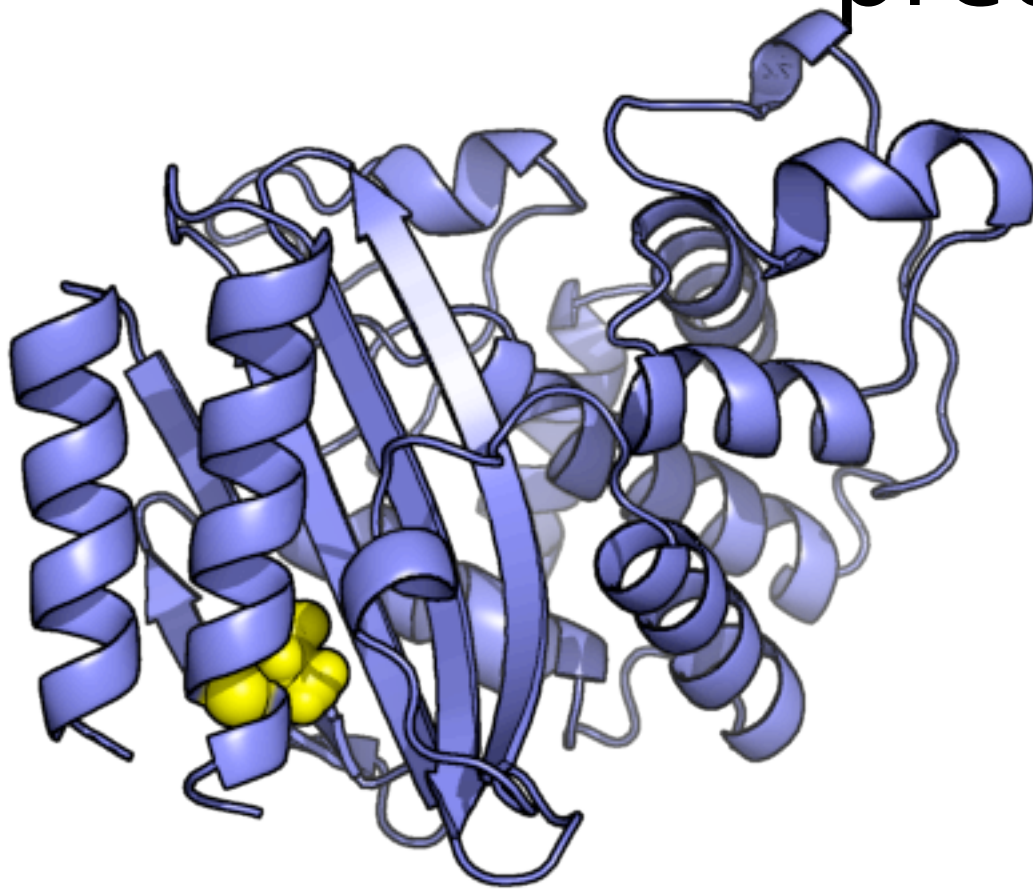
$$EX2 : k_{cl} \gg k_{int}$$

$$k_{obs} = \frac{k_{op} \times k_{int}}{k_{cl}} = K_{op} \times k_{int}$$

DTNB

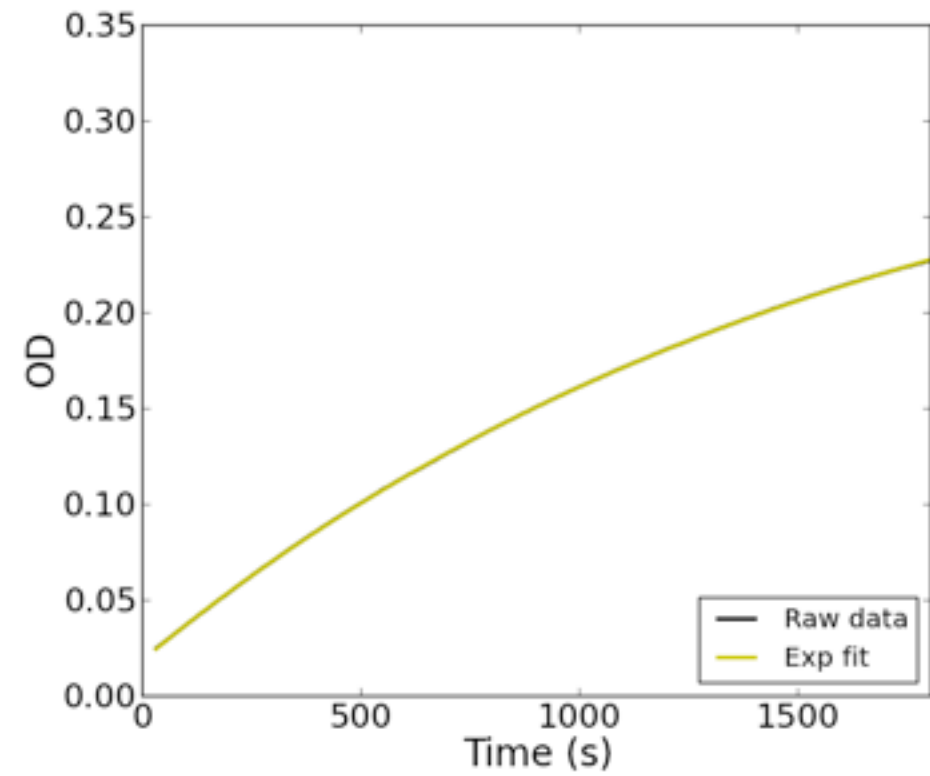
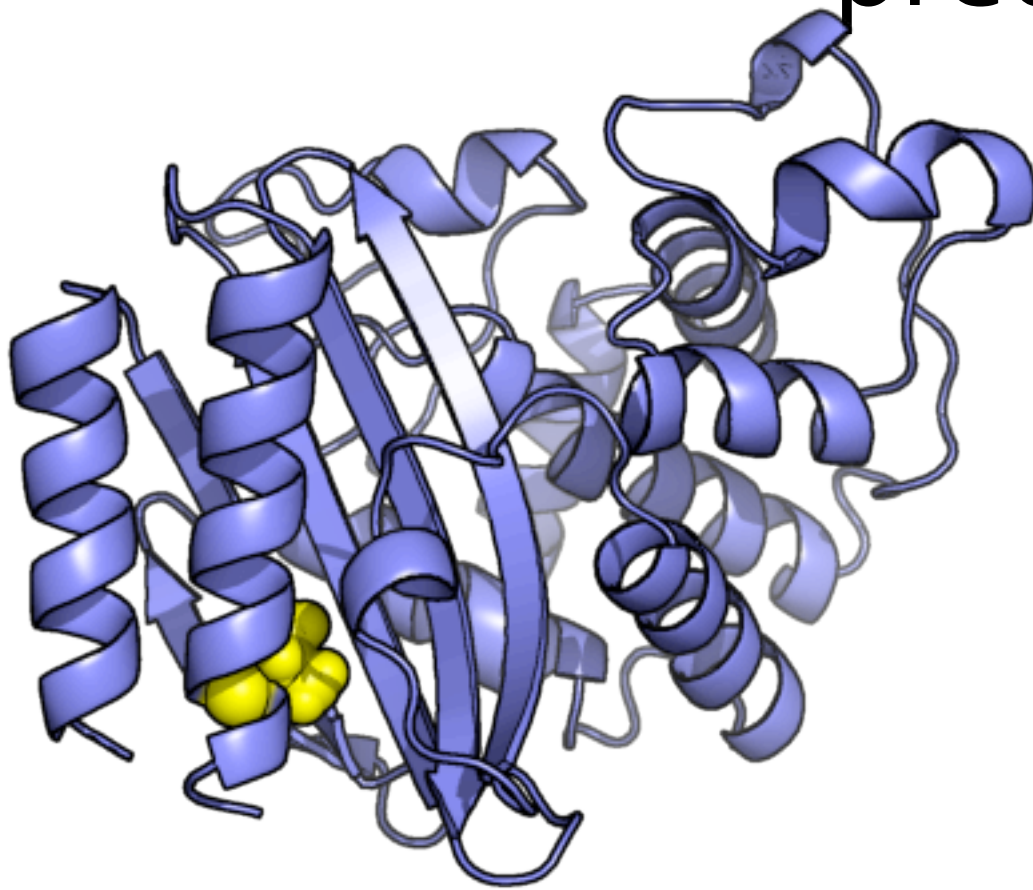


The known pocket also opens, as  
predicted

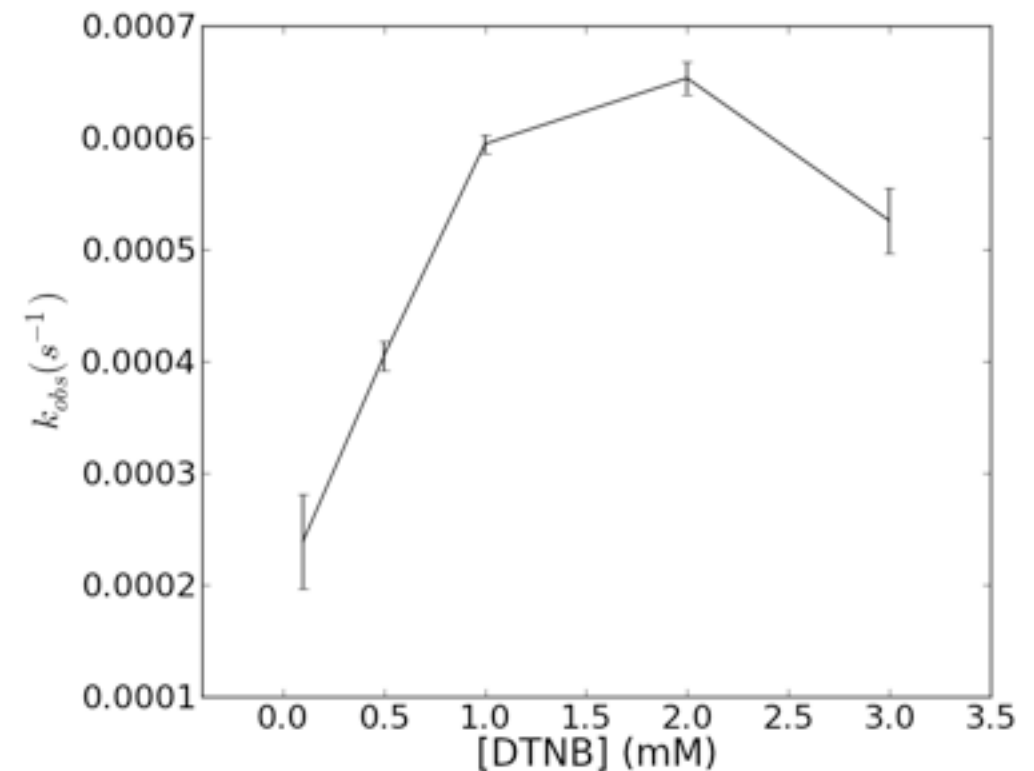
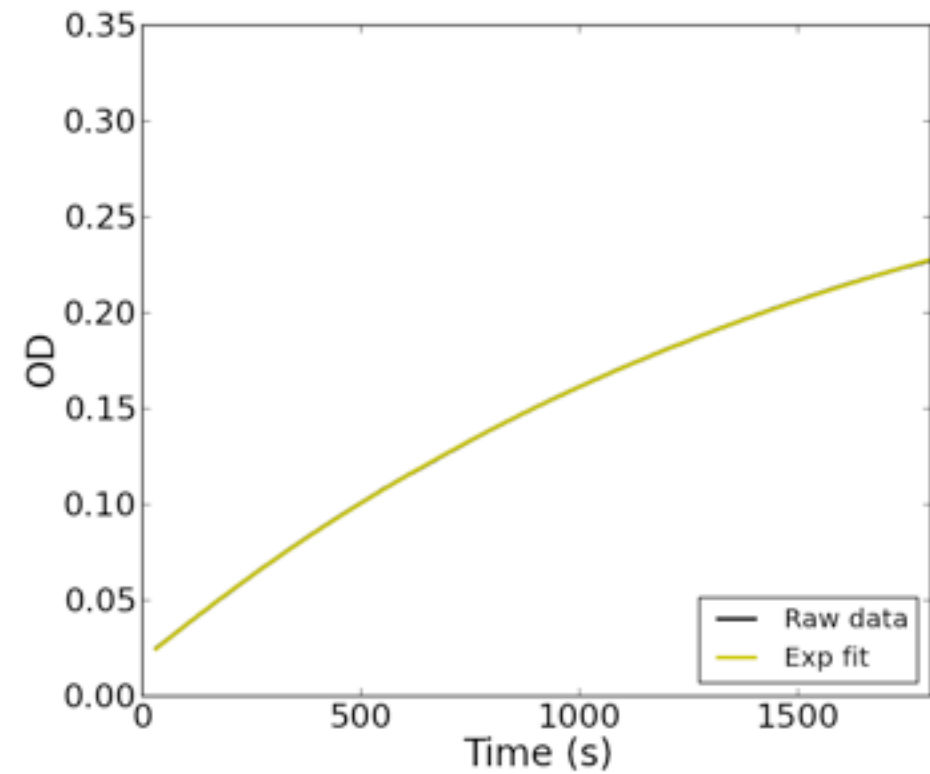
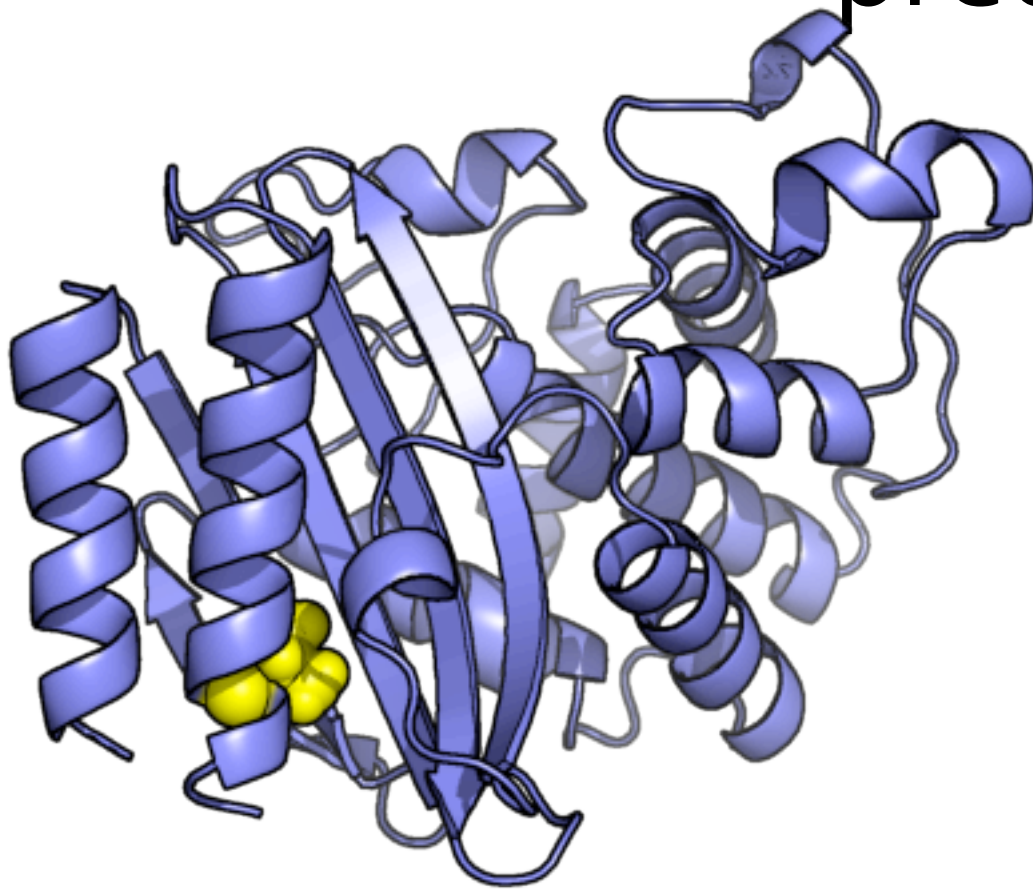
A 3D ribbon diagram of a protein structure, colored in light blue. The protein is shown in a complex, folded state. A yellow, multi-lobed ligand is bound within a pocket of the protein. A white arrow points from the ligand towards the right, indicating a predicted conformational change or movement of the protein structure. The background is white.



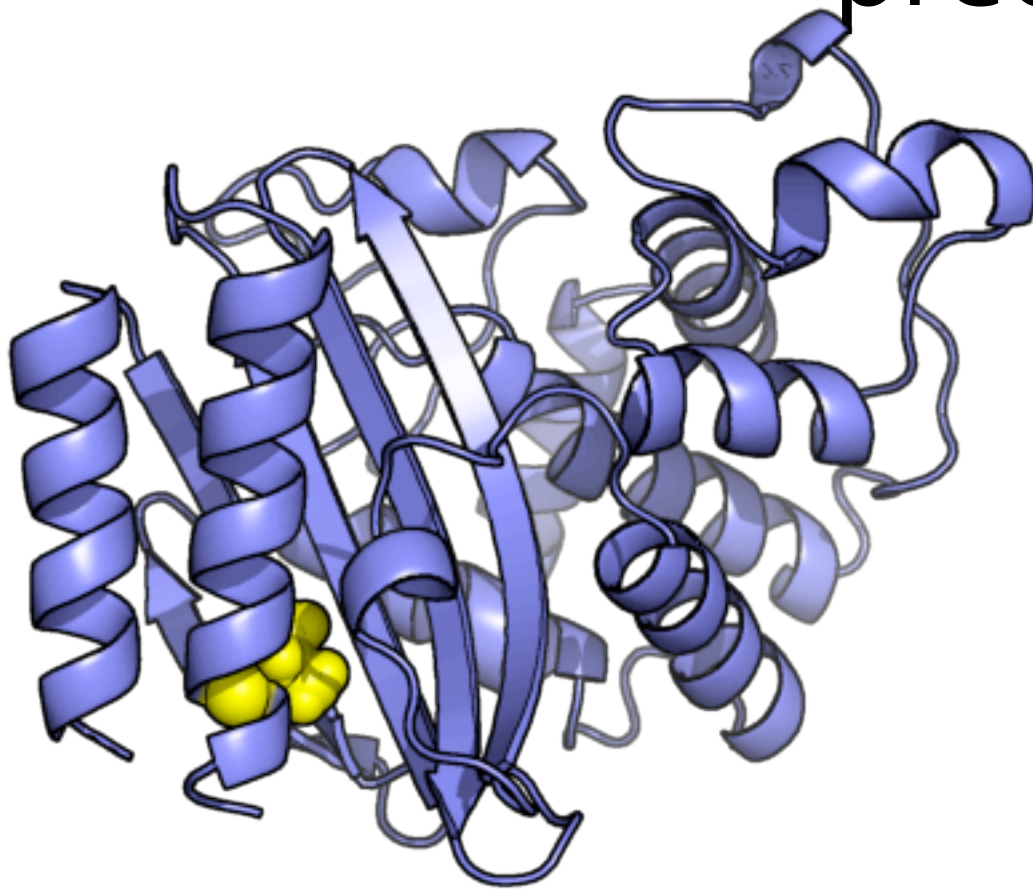
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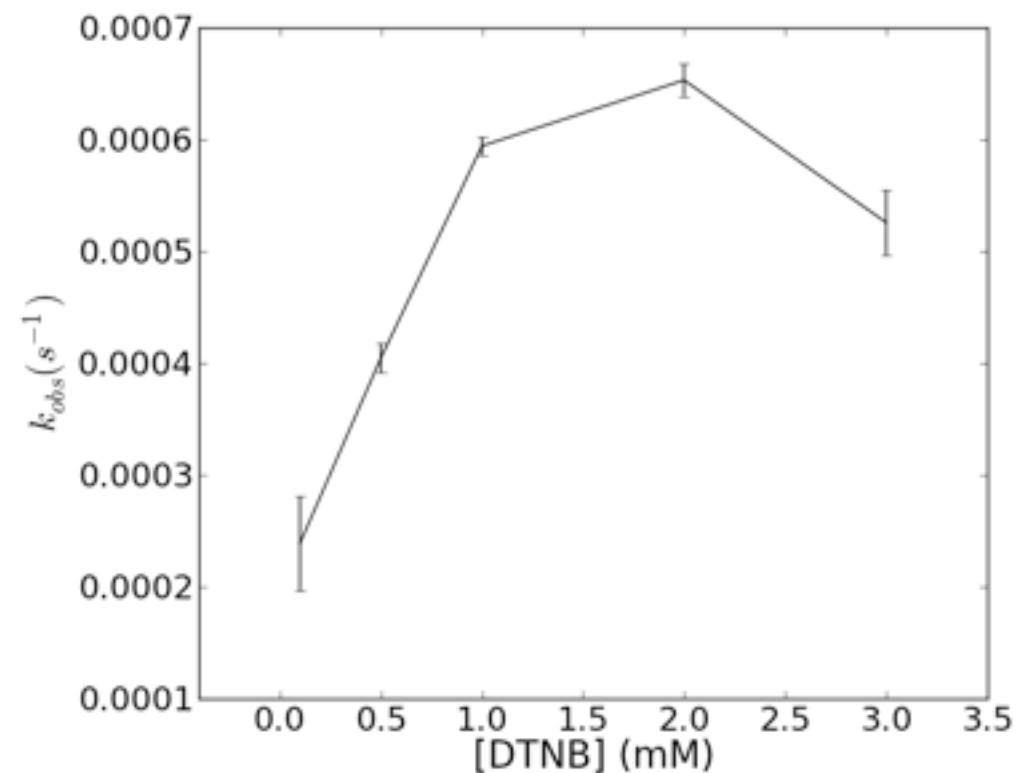
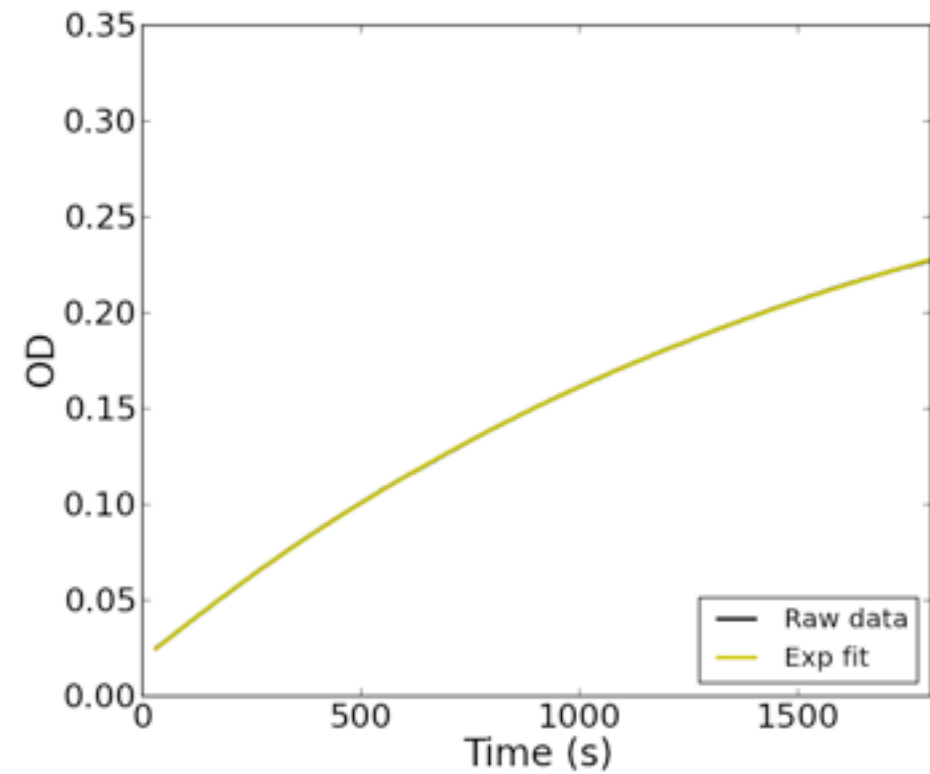
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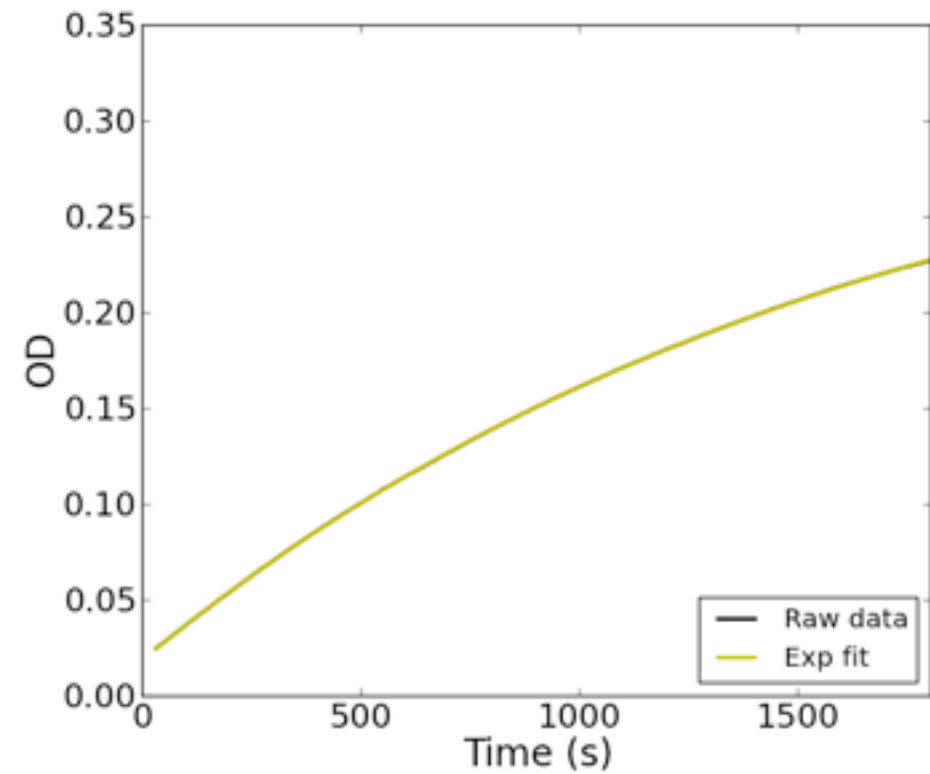
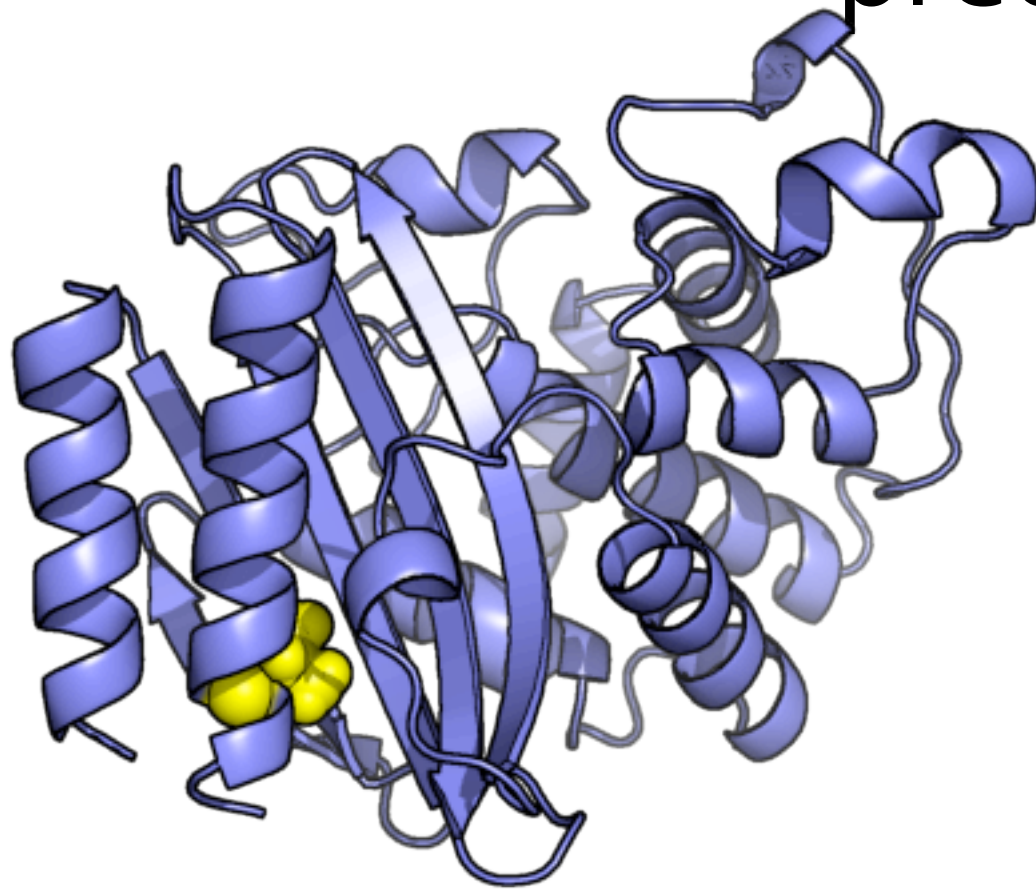
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Rate labeling:  $6 \times 10^{-4} \text{ s}^{-1}$

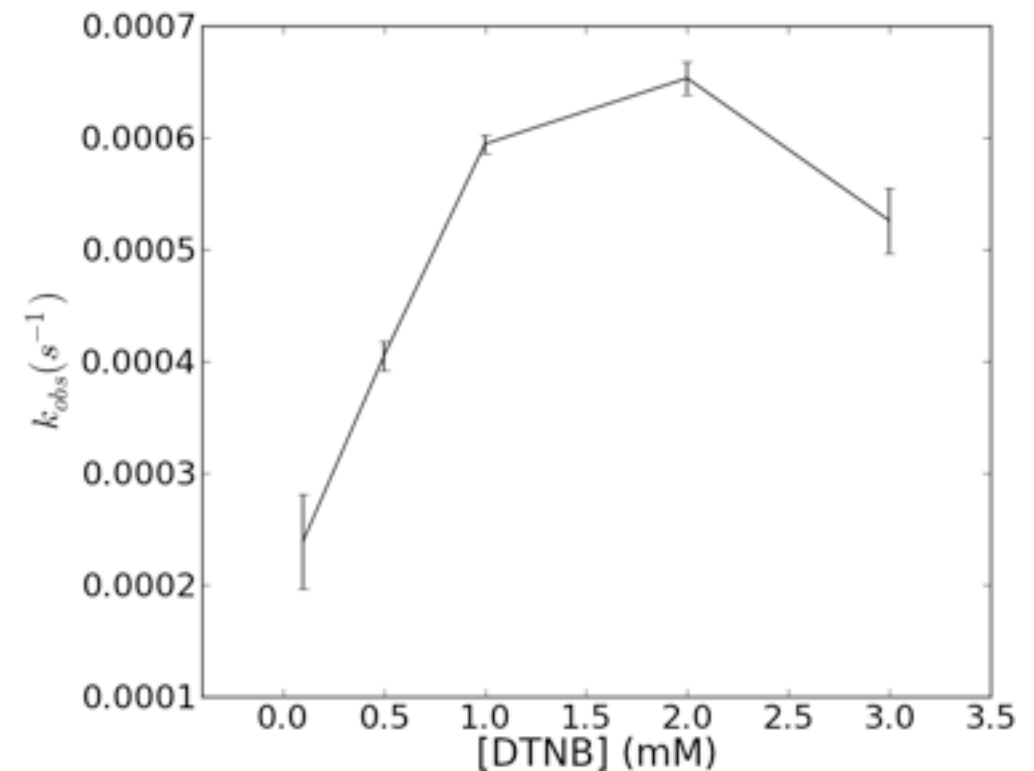


The known pocket also opens, as  
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Rate labeling:  $6 \times 10^{-4} \text{ s}^{-1}$

Rate unfolding  $< 2.5 \times 10^{-5} \text{ s}^{-1}$

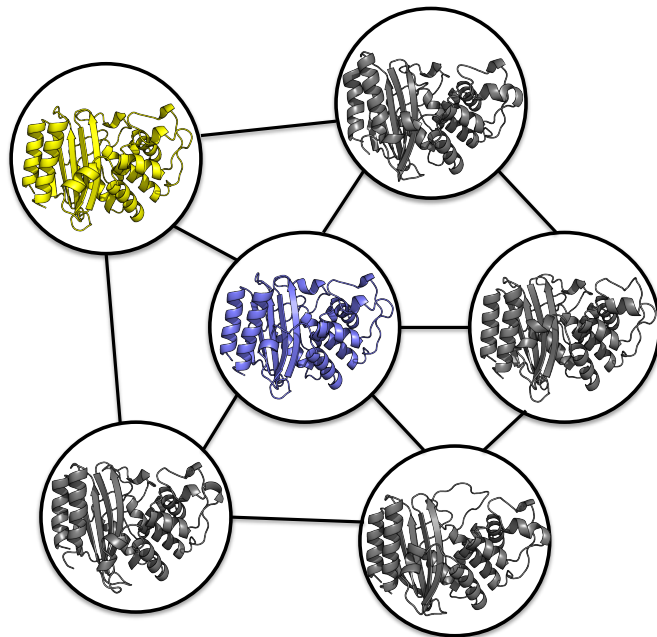


We are also testing a newly predicted  
pocket

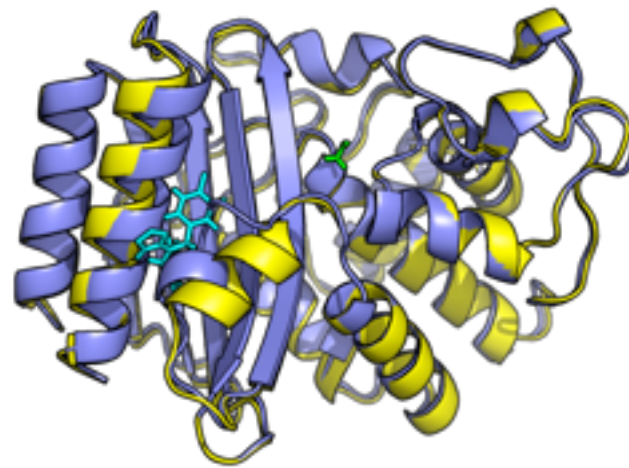
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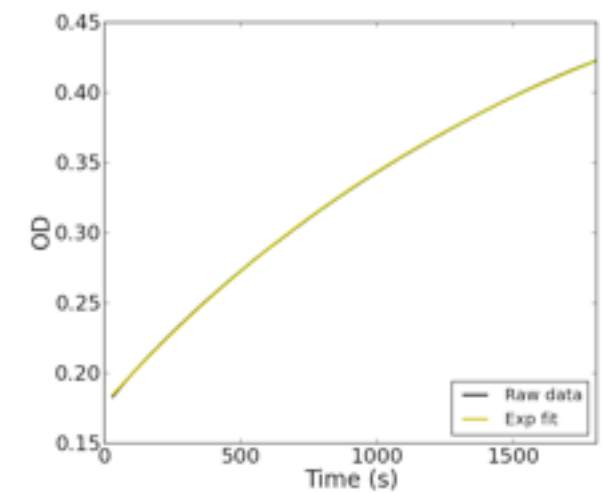
# Outline



Computational  
approach



Understanding  
and predicting  
allostery

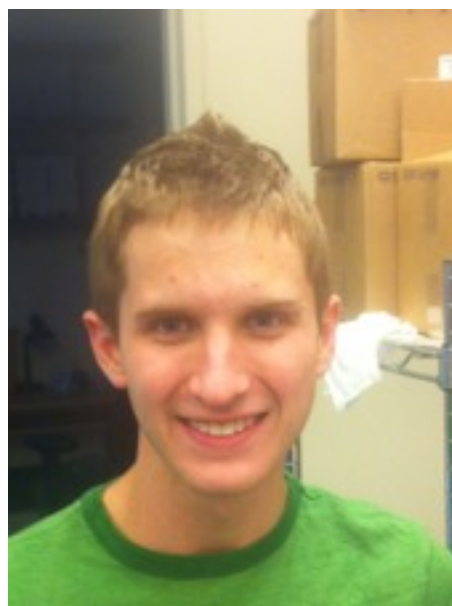


Experimental  
tests

# Thanks!



Brendan Maguire



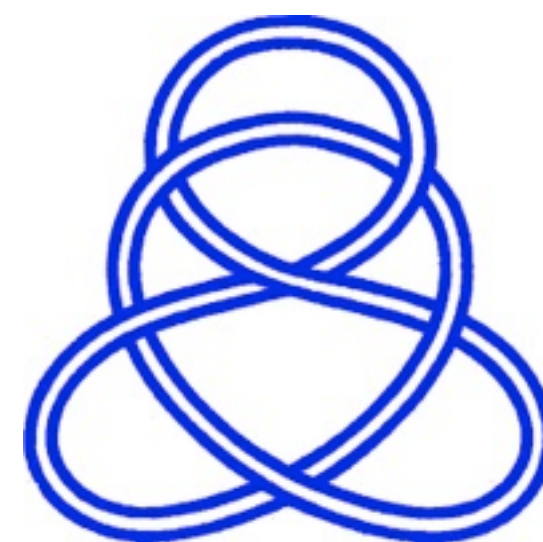
Eric Bolin



Susan Marqusee



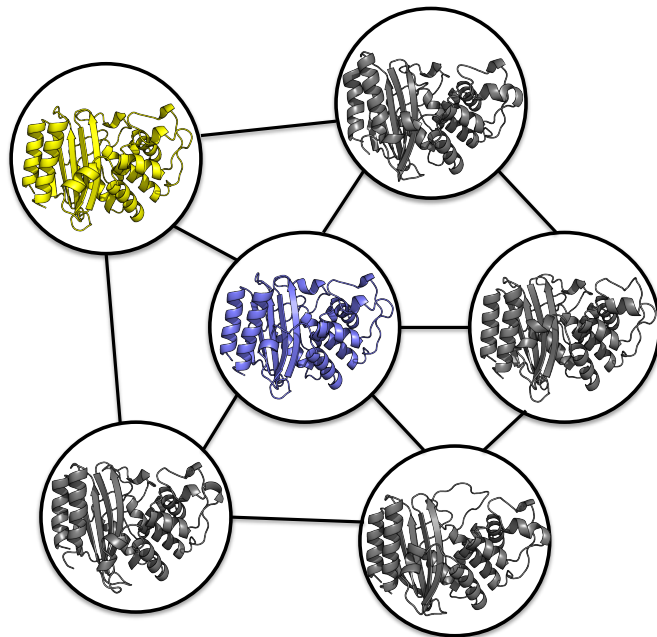
Phillip Geissler



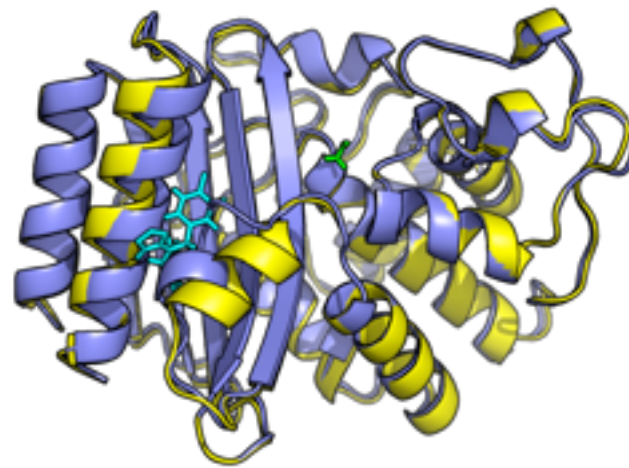
Miller Institute for  
Basic Research in  
Science



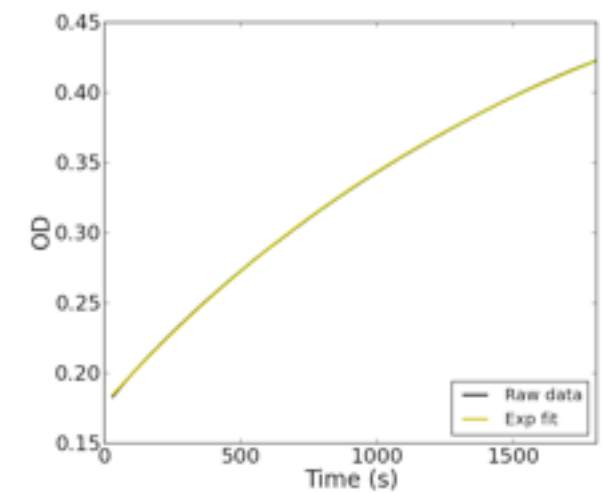
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